

Chapter 3

Modeling Work

3.1 Yield Strength Models

3.1.1 Introduction

The conventional method for developing a new weld metal with desired mechanical properties involves the design of a series of weld metals, varying chemical compositions and welding parameters. These welds are then manufactured and tested. A choice is then made of a particular combination of variables which best meets the requirements. Cost and time savings might be achieved with the help of appropriate models which reduce the number of steps needed.

The physical models discussed in Chapter 2, based on strengthening mechanisms, are not sufficiently sophisticated to enable a proper treatment of the problem. At the same time linear regression methods are not capable of representing the real behavior which is far from linear when all the factors are taken into account. On the other hand, the neural network methods described in Chapter 2 is ideally suited to complex phenomena with many variables. In the present work, neural networks are used to model the yield strength of weld metal as a function of weld metal chemical composition, welding parameters and heat treatment conditions.

3.1.1.1 Experimental Data base

All of the data collected are from multi run weld deposits in which the joint is designed to minimize dilution from the base metal, to enable specifically the measurement of all weld metal properties. Furthermore, they all represent electric arc welds made using one of the following processes: manual metal arc (MMAW), submerged arc welding (SAW) and tungsten inert gas (TIG). The welding process itself was represented only by the level of heat input. This is because a large number of published papers did not specify welding parameters in sufficient detail to enable the creation of a dataset without missing values. Missing values cannot be tolerated in the method used here. If the effect of a welding process is not properly represented by the heat input

and chemical composition, then neglect of any important parameters will make the predictions more 'noisy'. As discussed below, the noise in the output was found to be acceptable; a greater uncertainty arises from the lack of a uniform coverage of the input space. The data were collected from a large number of sources [33] to [76].

The aim of the neural network analysis was to predict the yield strength as a function of a large number of variables, including the chemical composition, the welding heat input and any heat treatment. The yield strength database consists of 2121 separate experiments. Neural network methods used in this work cannot cope with missing values of any of the variables.

3.1.1.2 Yield Strength Database

Table 3.1 shows the range, mean and standard deviation of each variable including the output(yield strength). The purpose here is simply to list the variables and provide an idea of the range covered. It is emphasized however, that unlike linear regression analysis, the information in Table3.1 cannot be used to define the range of applicability of the neural network model. This is because the inputs are in general expected to interact. We shall see later that it is the Bayesian framework of our neural network analysis which allows the calculation of error bars which define the range of useful applicability of the trained network. A visual impression of the spread of data is shown in Fig. 3.1. It can be concluded from Figure. 4.1(a to q) and Figure. 4.2(a to q) that the effect of Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Titanium, Boron, Niobium, Heat_input, Interpass_temperature, Post- weld heat treatment temperature and Post-weld heat treatment time on the Yield Strength of Ferritic Steel Welds have been systematically studied by both the methods BNN and GRNN.[27]

It can be concluded from Figure. 4.3.1 to 4.3.18 that the effect in combination of any two input variables (Independent variables) from Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Titanium, Boron, Niobium, Heat_input, Interpass_temperature, Post- weld heat treatment temperature and

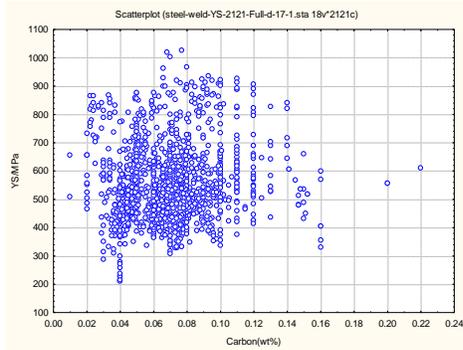
Post-weld heat treatment time on the Yield Strength of Ferritic Steel Welds have been systematically studied by GRNN method.

The prediction of the all Input variables for Targeted Yield Strength by Genetic Algorithms are given in Table 3.4. These can be useful for design of the Ferritic Steel Welds. Genetic Algorithms can be design the Ferritic Steel Welds by extrapolation beyond the existing data.

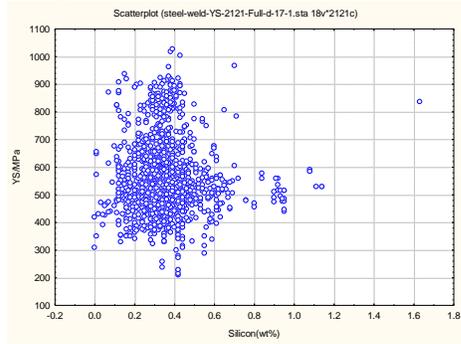
Table 3.1 The Input Variables for Yield Strength Model. “p.p.m .’ corresponds to parts per million by weight.

Variables	Min	Max	Average	StDev
C wt%	0.01	0.22	0.0708	0.0216
Si wt%	0	1.63	0.3467	0.1262
Mn wt%	0.23	2.31	1.1959	0.4175
S wt%	0.001	0.14	0.0081	0.0051
P wt%	0.001	0.25	0.0108	0.0075
Ni wt%	0	10.66	0.5807	1.4971
Cr wt%	0	12.1	0.6243	1.5961
Mo wt%	0	2.4	0.2001	0.3591
V wt%	0	0.32	0.0191	0.0507
Cu wt%	0	2.18	0.0659	0.2062
Ti ppm	0	1000	78.6382	122.4481
B ppm	0	200	9.2504	27.9733
Nb ppm	0	1770	53.7704	145.3195
HI kJ mm-1	0.55	7.9	1.3573	0.9931
IPT C	20	375	205.4668	42.7739
PWHTT C	20	780	328.1428	211.1714
PWHTt h	0	50	9.4335	6.5893
YS MPa	210	1026	535.7139	119.8611

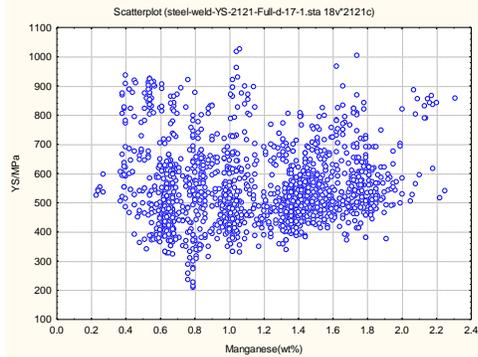
Scatter Plots of Yield Strength Data – 2121



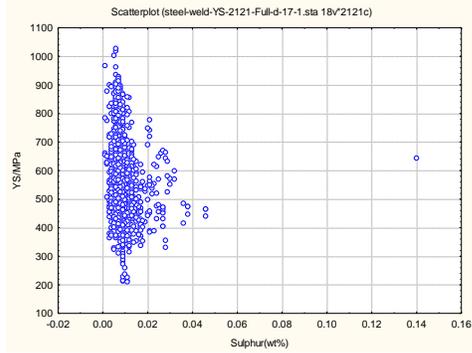
Yield Strength(MPa) – Carbon(wt %)



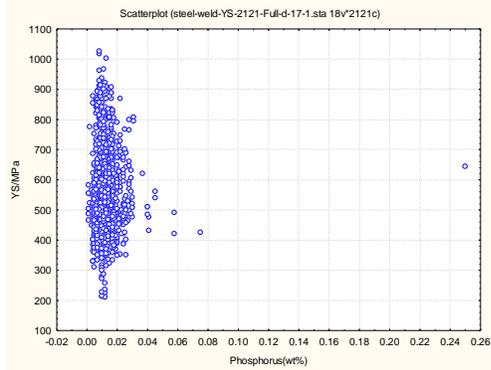
Yield Strength(MPa) – Silicon(wt %)



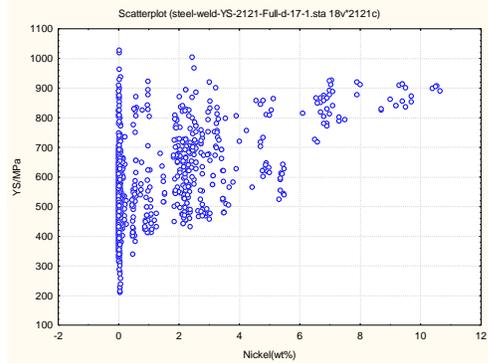
Yield Strength(MPa) – Manganese(wt %)



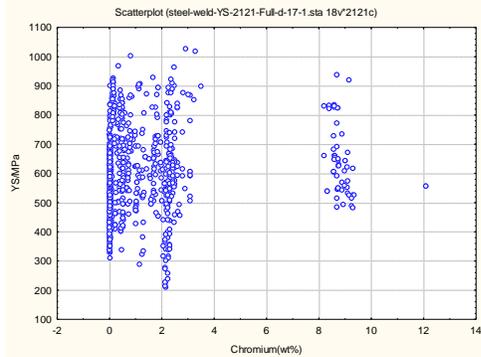
Yield Strength(MPa) – Sulphur(wt %)



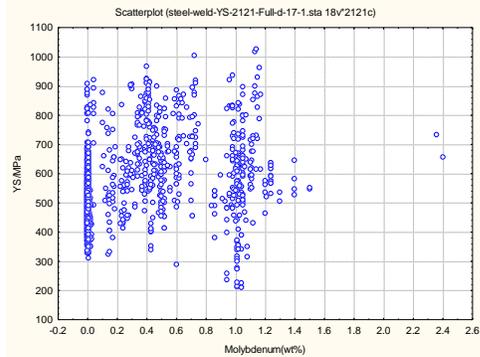
Yield Strength(MPa) – Phosphorus(wt %)



Yield Strength(MPa) – Nickel(wt %)

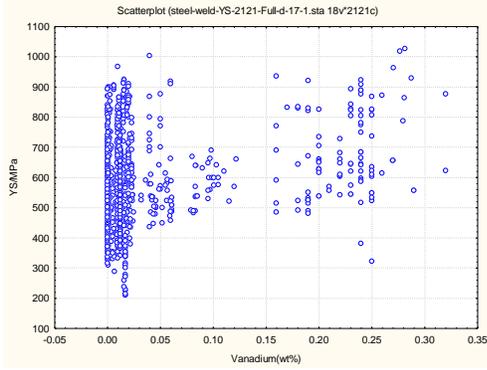


Yield Strength(MPa) – Chromium(wt %)

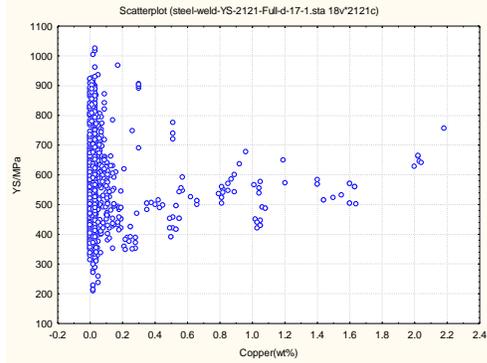


Yield Strength(MPa) – Molybdenum(wt %)

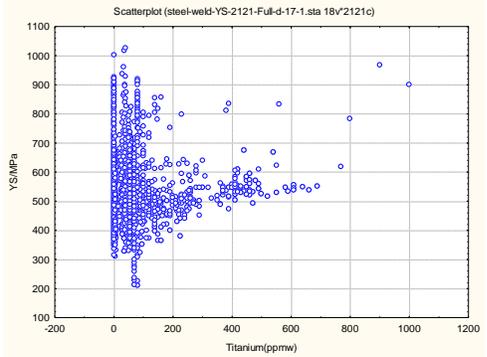
Scatter Plots of Yield Strength Data- 2121



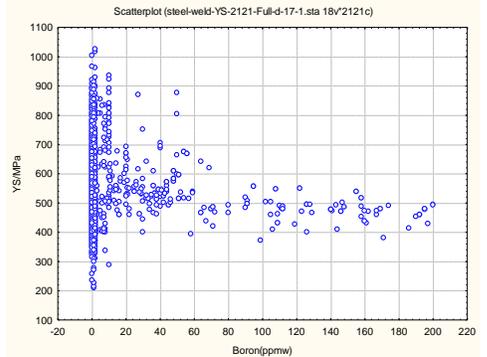
Yield Strength(MPa) – Vanadium(wt %)



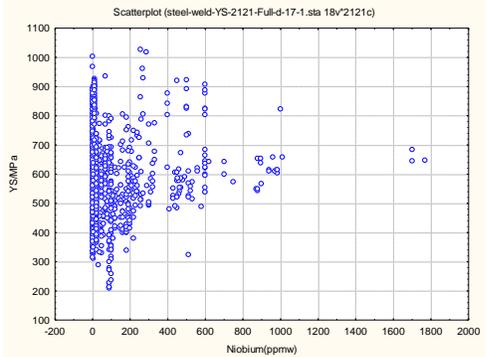
Yield Strength(MPa) – Copper(wt %)



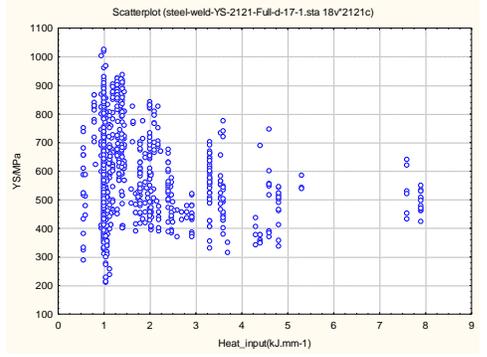
Yield Strength(MPa) – Titanium(ppm)



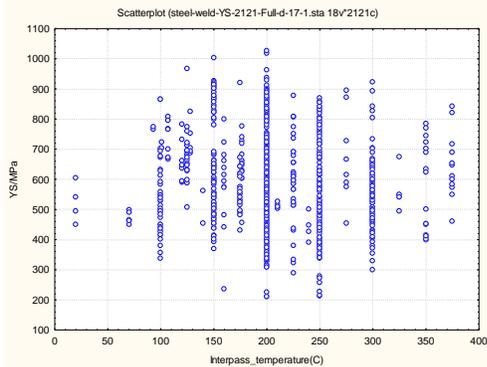
Yield Strength(MPa) – Boron(ppm)



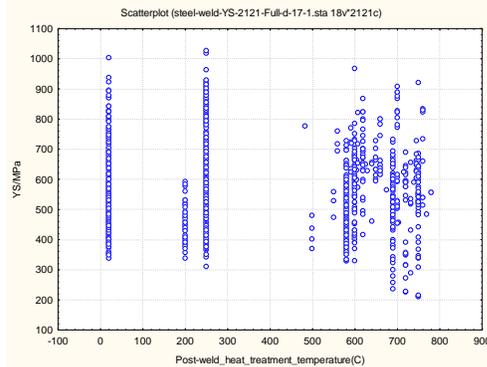
Yield Strength(MPa) – Niobium(ppm)



Yield Strength(MPa) – Heat Input(kJ mm-1)



Yield Strength(MPa) – Interpass_temperature(C)



Yield Strength(MPa) – Postweld_HT_Temp(C)

Scatter Plots of Yield Strength Data- 2121

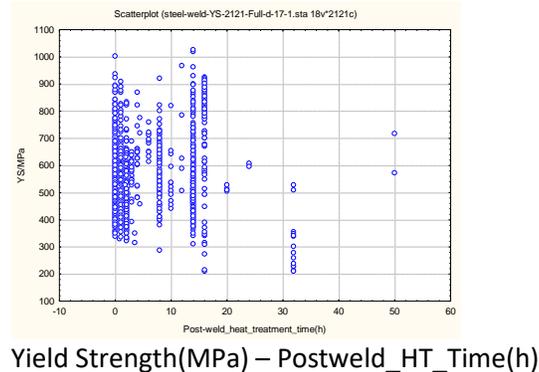


Figure 3.1 Database distribution used for yield strength model. “p.p.m .’ corresponds to parts per million by weight.

3.1.2 Neural Network Models for Yield Strength

3.1.2.1 Bayesian Neural Network Modeling and procedure

- 1 Data of yield strength were collected and plotted in the form of Scatter plots.
2. Data prepared according to the file format required to run in Neural Network Softwares.
(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)
3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)
4. Data of Ferritic Steel Weld Yield Strength 2121 run in NeuroMat Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.10

Neural network architecture for Bayesian Neural Network was set in NeuroMat Software :

Three layers : **Input Layer**(Input Variables), **Hidden Layer** (Algorithms) and **Output Layer** (Yield Strength)

Algorithms : Bigback 5

5. The data of Ferritic Steel Weld Yield Strength 2121 run in NeuroMat Software with above Neural network architecture for best Neural Network Committee model. The best committee model was decided on the basis of smallest test error of the committee model.

6. For best committee model, the data of Ferritic Steel Weld Yield Strength 2121 run in NeuroMat Software repeatedly hundred of times and finalise the best committee model with smallest test error. (NeuroMat gives in single run set of 100 models which required time in hours. Out of these 100 models, the models in the committee are selected on the basis of smallest test error. The number of models in committee varies everytime with repeatedly running the data in NeuroMat. Thus the selection of committee model with a smallest test error is time consuming.)

Some more than hundred yield strength neural network models were trained on a training dataset which consisted of a random selection of 70% of the data 1485 from the yield strength dataset. And 20% of the data 424 from yield strength data set was used for cross validation. The remaining 212 data formed the test dataset which was used to see how the model generalizes on unseen data. Each model contained the 17 inputs listed in Table 1 but with different numbers of hidden units or the random seeds used to initiate the values of the weights. Fig. 3.2 shows the results. As expected, the perceived level of noise (σ_y) in the normalised yield strength decreases as the number of hidden units increases, Fig. 3.2a. This is not the case for the test error, which goes through a minimum at five hidden units, Fig. 3.2b, and for the log predictive error which reaches a maximum at seventeen hidden units, Fig. 3.2c.

The error bars presented throughout this work represent a combination of the perceived level of noise σ_y in the output and the fitting uncertainty estimated from the Bayesian framework. It is evident that there are a few outliers in the plot of the predicted versus measured yield strength for the test dataset, Fig. 3.2f. Each of these outliers has been investigated and found to represent unique data which are not represented in the training dataset, Fig. 3.2e.

It is possible that a committee of models can make a more reliable prediction than an individual model (Chapter 2). The best models are ranked using the values of the log predictive errors Fig. 3.2c. Committees are then formed by combining the predictions of the best L models, where $L = 1, 2, \dots$; the size of the committee is therefore given by the value of L . A plot of the test error of

the committee versus its size gives a minimum which defines the optimum size of the committee, as shown in Fig. 3.2d. The test error associated with the best single model is clearly greater than that of any of the committees Fig. 3.2d. The committee with seven models was found to have an optimum membership with the smallest test error. The committee was therefore retrained on the entire data set without changing the complexity of any of its member models.

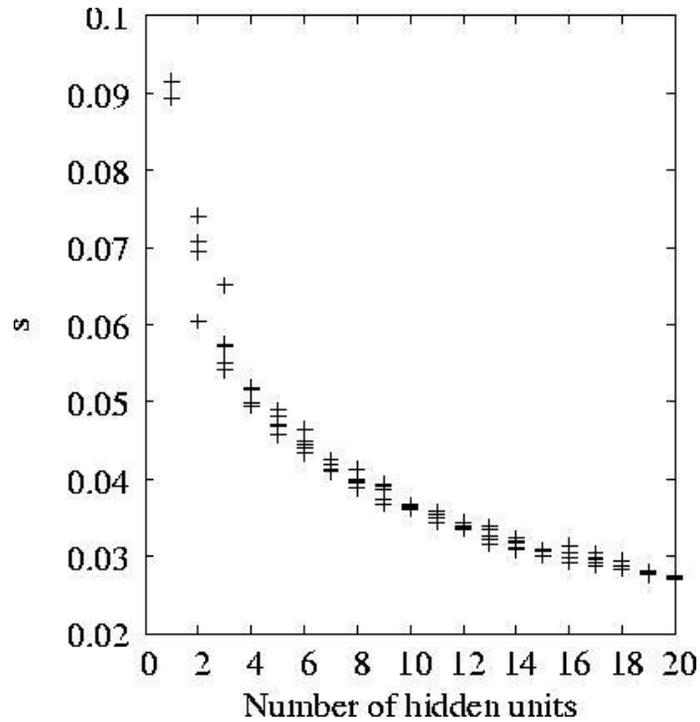


Figure 3.2(a) σ_y (sigma) vs Hidden units

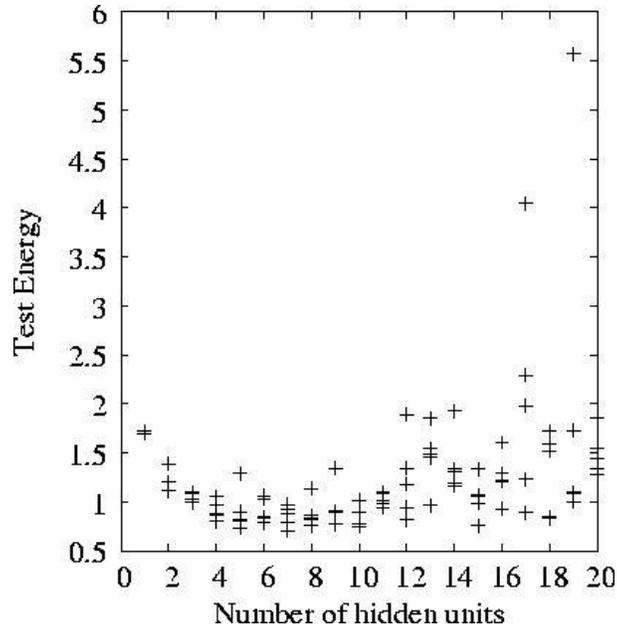


Figure 3.2(b) Test Error (Test Energy) vs Hidden units.

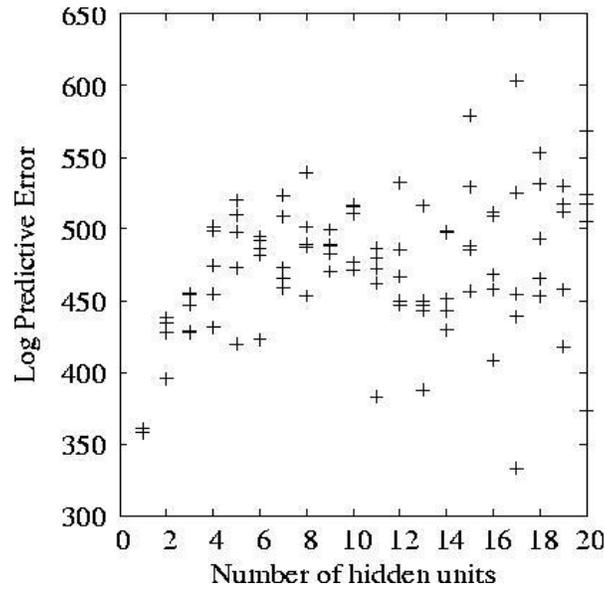


Figure 3.2(c) Log predictive error vs Hidden units

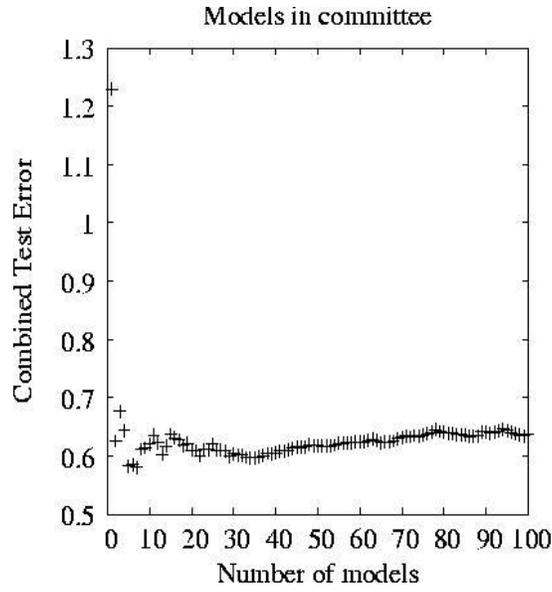


Figure 3.2(d) Test Error vs Models in committee

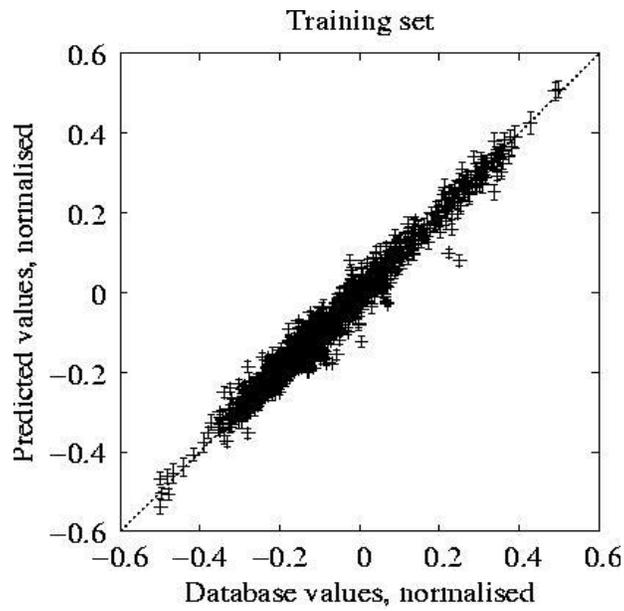


Figure 3.2(e) Predicted normalized Y.S. vs Measured normalized YS. (Training Dataset)

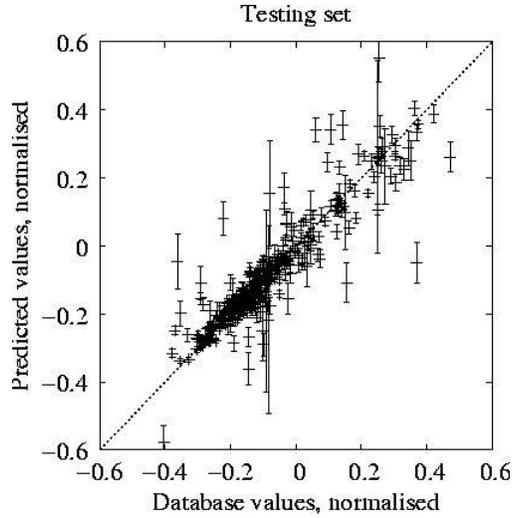


Figure 3.2 (f) Predicted normalized Y.S. vs Measured normalized YS. (Test Dataset)

Figure 3.2 (a to f) Yield Strength (YS) model features.

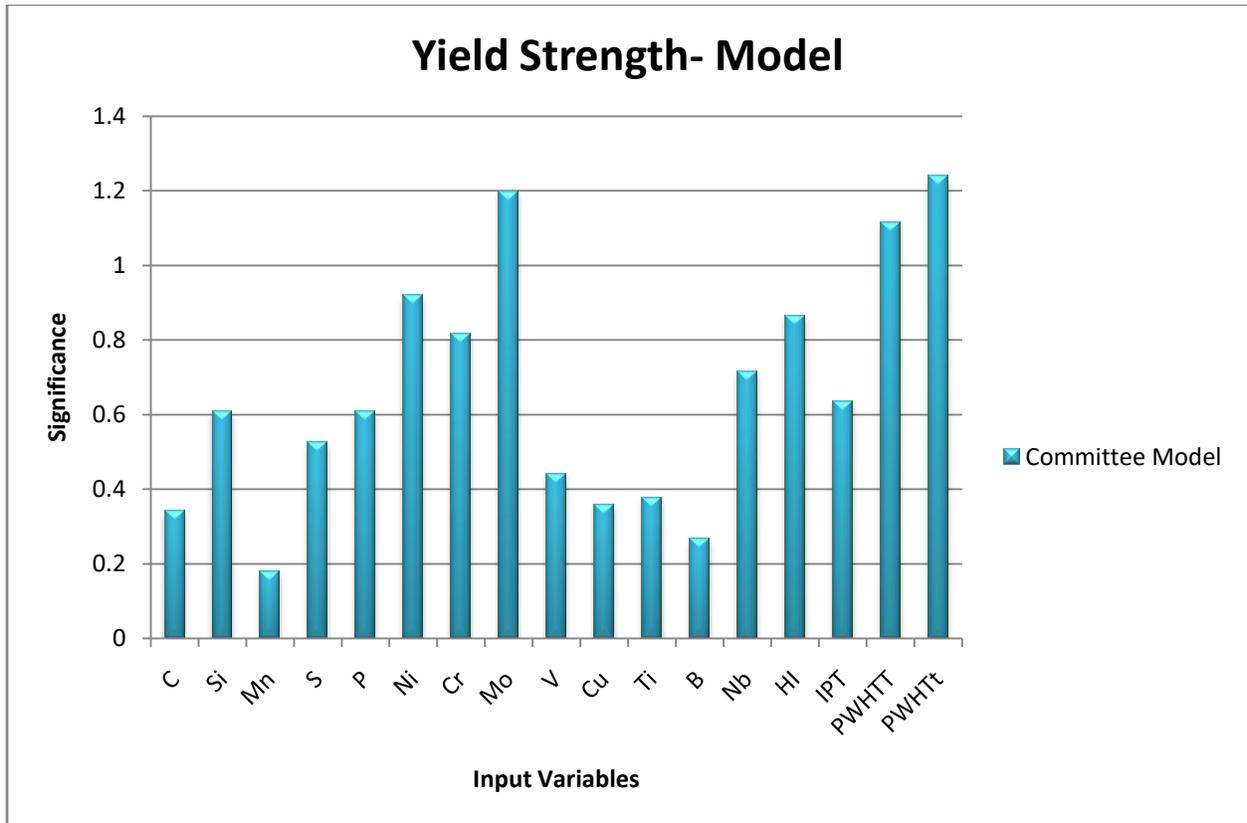


Figure 3.3 The perceived significance σ_w value of best seven yield strength models in a committee for each of the input variables.

Fig. 3.3 indicates the significance σ_w of each of the input variables, as perceived by first seven neural network models in the committee. The σ_w value represents the extent to which a particular input explains the variation in the output, rather like a particular correlation coefficient in linear regression analysis. The post-weld heat treatment time on the whole explains a large proportion of variation in the yield strength Figure. 3.3. All variables considered are found to have a significant effect on the output indicating a good choice of inputs.

3.1.3 Comparison of Neural network models and procedure (MLP, RBF, and GRNN)

- 1 Data of yield strength were collected and plotted in the form of Scatter plots.
2. Data prepared according to the file format required to run in Neural Network Softwares.

(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)

3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)

4. Data of Ferritic Steel Weld Yield Strength 2121 run in Statistica Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.11

Neural network architecture was set in Statistica software for MLP, RBF and GRNN :

MLP 17:17-10-1:1 Algorithms : BP100,CG20,CG18b

RBF 17:17-530-1:1 Algorithms : SS,KN,PI

GRNN 17:17-1061-2-1:1 Algorithms : SS

BP Back propagation, CG Conjugate gradient descent, SS (sub) sample, KN K-nearest neighbor (deviation assignment), PI Pseudo-invert (linear least squares), b Best network (the network with lowest selection error in the run was restored)

A neural network's architecture is of form I:N-N-N:O, where I is the number of input variable, O the number of output variables, N the number of units in each layer.

5. The data of Ferritic Steel Weld Yield Strength 2121 run in Statistica Software with above Neural network architecture for best Neural Network model in all three MLP, RBF and GRNN.

6. For best model, the data of Ferritic Steel Weld Yield Strength 2121 run in Statistica Software repeatedly hundred of times and finalise the best Neural Network model with smallest training error in all three MLP, RBF and GRNN.

7. The neural network model with the smallest training error was the GRNN model.

Table 3.2 shows the comparison of selected Neural Network models on the basis of their Training Errors. The GRNN models have lowest Training Errors for Yield Strength of Ferritic Steel Welds. The GRNN models are selected for modeling from three basic neural network methods (MLP, RBF, and GRNN). Statistica 7.1 software is used for MLP, RBF and GRNN.

Table 3.2 Comparison of Neural network models {MLP, RBF, GRNN}

Yield Strength Models				
MLP	Train Error	Test Error	Training/Members	Remarks
MLP 17:17-10-1:1 (Model:No.05)	0.062442	0.078690	BP100,CG20,CG18b	1 Hidden layer
MLP 17:17-13-6-1:1 (Model:No.25)	0.058963	0.067180	BP100,CG20,CG59b	2 Hidden layers
MLP 17:17-6-8-13-1:1 (Model:No.14)	0.058458	0.065638	BP100,CG396b	3 Hidden layers
MLP 17:17-14-9-1:1 (Model:No.07)	0.036248	0.063303	BP100,CG458b	2 Hidden layers
MLP 17:17-9-14-1:1 (Model:No.10)	0.047847	0.058474	BP100,CG492b	2 Hidden layers
MLP 17:17-6-7-1:1 (Model:No.18)	0.054954	0.065891	BP100,CG353b	2 Hidden layers
Yield Strength Models				
RBF	Train Error	Test Error	Training/Members	Remarks
RBF 17:17-530-1:1 (Model:No.10)	0.001791	0.002782	SS,KN,PI	1 H layer
Yield Strength Models				
GRNN	Train Error	Test Error	Training/Members	Remarks
GRNN 17:17-1061-2-1:1 (Model:No.21)	0.000668	0.004186	SS	2 H layer
Note: See Appendix C for Profile String of Statistical Neural Network Software				

3.1.4 Best GRNN Model for the Yield Srength

The normal behaviour of the Predicted Yield Strength and Observed Yield Strength are observed in the Figure. 3.4 for Training data, Validation data and Testing data. Training of the model is excellent by GRNN method.

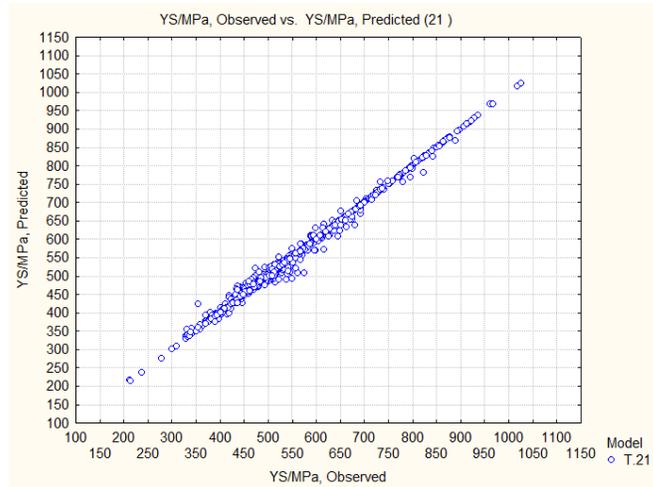


Figure a Training Data for GRNN model of Yield Strength

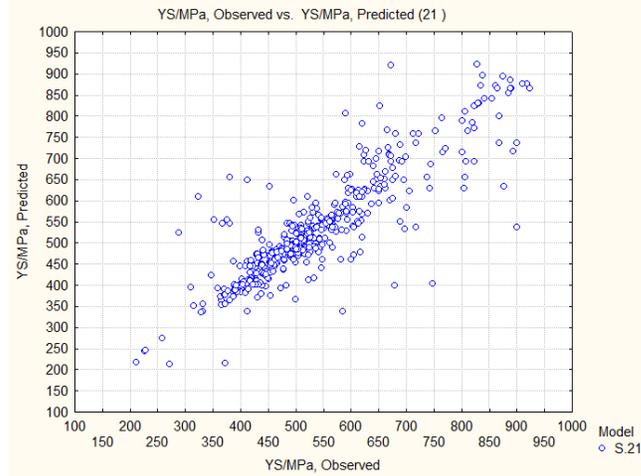


Fig b Validation Data for GRNN model of Yield Strength

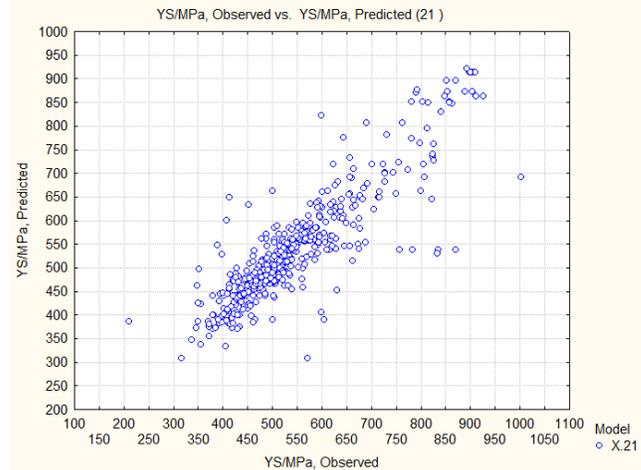


Fig c Test Data for GRNN model of Yield Strength

Figure 3.4 (a to c) Training data, validation data and test data of the Best GRNN model for Yield Strength.

The best model of GRNN has training error 0.000668, validation error (selection error) 0.004426, and testing error 0.004186. This model is used for getting the results in form of various response graphs to understand the trend between the input variables and output variable (Yield Strength).(Figure 4.2)

Table 3.3 Comparison of Significance of Best Trained Models of Yield Strength

Input Variables	Significance GRNN Model	Significance BNN Model
Carbon(wt%)	7	15
Silicon(wt%)	11	9
Manganese(wt%)	3	17
Sulphur(wt%)	17	11
Phosphorus(wt%)	16	10
Nickel(wt%)	1	4
Chromium(wt%)	6	6
Molybdenum(wt%)	4	2
Vanadium(wt%)	5	12
Copper(wt%)	13	14
Titanium(ppm)	14	13
Boron(ppm)	15	16
Niobium(ppm)	10	7
Heat_input(kJ.mm-1)	12	5
Interpass_temperature(C)	8	8
Postweld_heat_treatment_temperature(C)	2	3
Post-weld_heat_treatment_time(h)	9	1

Table 3.3 shows the comparison of Significance of the GRNN and BNN models. Number 1 indicates highest value of significance and Number 17 lowest value of significance. Most of the Input Variables are closer in significance for both the models. All input variables considered are found to have a significant effect on the output indicating a good choice of inputs.

3.1.5 Neural Network and Genetic Algorithms Modelling for Yield Strength of Ferritic Steel Welds

3.1.5.1 Genetic Algorithms parameters and procedure

A genetic algorithm has been developed in language C considering the following parameters:

Number of populations = 3

Number of generations = 3000

Population size = 20 chromosomes

When a new generation is created, the following steps are followed: after ranking the 20 chromosomes according to their scores, the first chromosome is copied without change. The chromosomes 2 to 19 are recombined with each others. One gene of one of these chromosomes is mutated between $\pm 0.2\%$. The chromosome 20, with the worst score, is killed and a new random chromosome is generated and incorporated in the new population.

This program can calculate the best set (x_1, x_2, \dots, x_j) of input parameters for a desired output y , which is in this study, the yield strength of ferritic steel welds, for which a Bayesian neural network model was developed[32].

The steps for Genetic Algorithms Modelling:

- First, all the files related to the neural network created for the yield strength were put in the folder "gacode" to optimise. These files were the following:

```
generate44.exe  
norm_test.in  
_w*f  
*.lu  
specl.tl  
outran.x  
MINMAX
```

- Then, the labels of the inputs variables of the neural network were written in the "labels.tct" file
- Then the all inputs variables were define in the "values" file to vary.
- Then, the desired target value of yield strength was normalised and entered it in the "nninput" file, as well as the wanted accuracy.
- Finally, the C program "ga_code" was compiled and executed.

After execution of the Genetic Algorithms program, the output was the values of 17 input variables for given target value of the yield strength of Ferritic Steel Weld. The calculation time was in hours.

Three different target values of Ferritic Steel Weld's yield strengths were taken and Genetic Algorithms programs were run. The outputs were given in result and discussion Chapter 4.

3.2 Ultimate Tensile Strength Models

3.2.1 Experimental Data base

All of the data collected are from multi run weld deposits in which the joint is designed to minimize dilution from the base metal, to enable specifically the measurement of all weld metal properties. Furthermore, they all represent electric arc welds made using one of the following processes: manual metal arc (MMAW), submerged arc welding (SAW) and tungsten inert gas (TIG). The welding process itself was represented only by the level of heat input. This is because a large number of published papers did not specify welding parameters in sufficient detail to enable the creation of a dataset without missing values. Missing values cannot be tolerated in the method used here. If the effect of a welding process is not properly represented by the heat input and chemical composition, then neglect of any important parameters will make the predictions more 'noisy'. As discussed below, the noise in the output was found to be acceptable; a greater uncertainty arises from the lack of a uniform coverage of the input space. The data were collected from a large number of sources [33] to [76]. The aim of the neural network analysis was to predict the ultimate tensile strength as a function of a large number of variables, including the chemical composition, the welding heat input and any heat treatment. The ultimate tensile strength database consists of 2091 separate experiments. Neural network methods used in this work cannot cope with missing values of any of the variables.

3.2.1.1 Ultimate Tensile Strength Database

Table 3.4 shows the range, mean and standard deviation of each variable including the output (ultimate tensile strength). The purpose here is simply to list the variables and provide an idea of the range covered. It is emphasized however, that unlike linear regression analysis, the information in Table 3.4 cannot be used to define the range of applicability of the neural network model. This is because the inputs are in general expected to interact. We shall see later that it is the Bayesian framework of our neural network analysis which allows the calculation of error

bars which define the range of useful applicability of the trained network. A visual impression of the spread of data is shown in Fig. 3.5. It can be concluded from Figure. 4.4(a to r) and Figure. 4.5(a to r) that the effect of Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Oxygen, Titanium, Boron, Niobium, Heat input, Interpass_temperature, Post- weld heat treatment temperature and Post-weld heat treatment time on the Ultimate Tensile Strength of Ferritic Steel Welds have been systematically studied by BNN and GRNN.[27]

It can be concluded from Figure. 4.6.1 to 4.6.19 that the effect in combination of any two input variables (Independent variables) from Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Oxygen, Titanium, Boron, Niobium, Heat_input, Interpass_temperature, Post- weld heat treatment temperature and Post-weld heat treatment time on the Ultimate Tensile Strength of Ferritic Steel Welds have been systematically studied by GRNN.

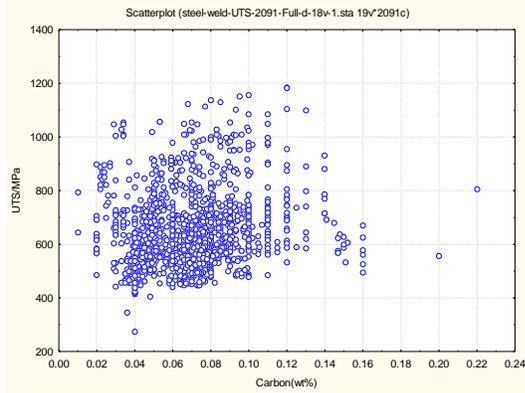
The prediction of the all Input variables for Targeted Ultimate Tensile Strength by Genetic Algorithms are given in Table 4.4 . These can be useful for the design of the Ferritic Steel Welds. Genetic Algorithms can design the Ferritic Steel Welds by extrapolation beyond the existing data.

Table 3.4: The Input Variables for Ultimate Tensile Strength Model.

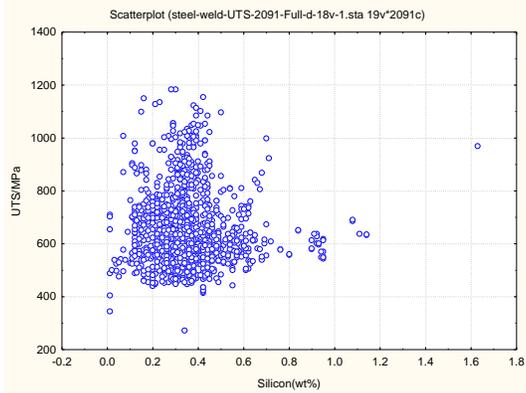
Variables	Min	Max	Average	StDev
C wt%	0.01	0.22	0.0705	0.021
Si wt%	0.01	1.63	0.3477	0.1283
Mn wt%	0.23	2.31	1.1955	0.4156
S wt%	0.001	0.14	0.008	0.0051
P wt%	0.001	0.25	0.0107	0.0073
Ni wt%	0	10.66	0.581	1.5071
Cr wt%	0	12.1	0.5869	1.4827
Mo wt%	0	2.4	0.1988	0.3606
V wt%	0	0.32	0.0187	0.0506
Cu wt%	0	2.18	0.0597	0.1953
O ppm	0	1650	377.6982	166.9297
Ti ppm	0	1000	80.0548	124.85
B ppm	0	200	9.3161	28.1533
Nb ppm	0	1770	51.1751	141.6126
HI kJ mm ⁻¹	0.55	7.9	1.3392	0.9366
IPT C	20	375	206.4539	41.9047
PWHTT C	20	770	333.6054	206.2762
PWHTt h	0	50	9.7532	6.5109
UTS MPa	273	1184	621.2198	123.4969

("p.p.m ." corresponds to parts per million by weight.)

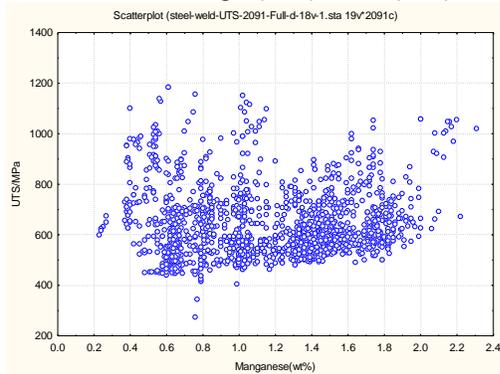
Scatter Plots of Ultimate Tensile Strength-Data-2091



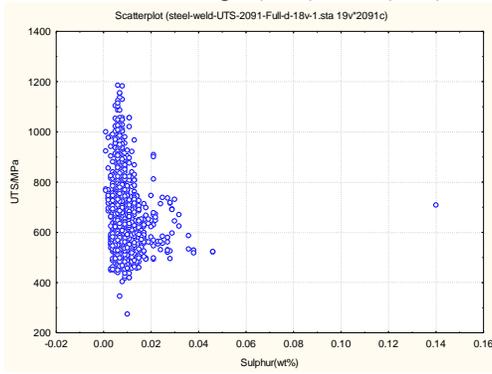
Ultimate Tensile Strength (MPa)-Carbon(wt%)



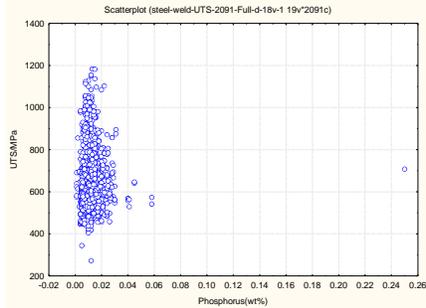
Ultimate Tensile Strength (MPa)-Silicon(wt%)



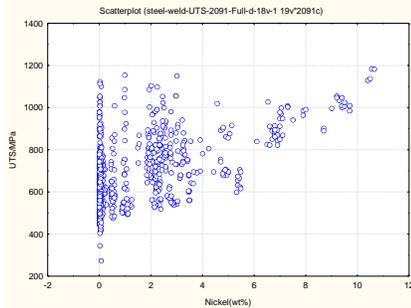
Ultimate Tensile Strength (MPa)-Manganese(wt%)



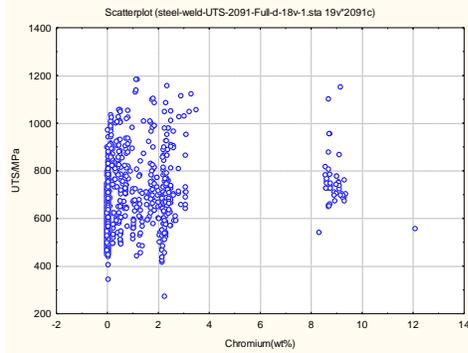
Ultimate Tensile Strength (MPa)-Sulphur(wt%)



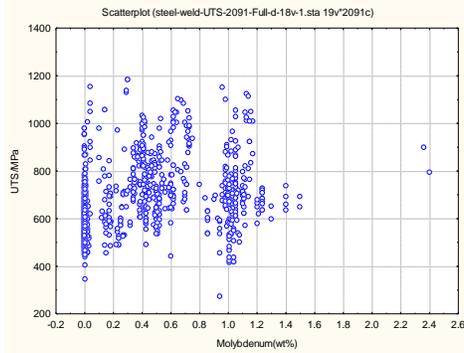
Ultimate Tensile Strength (MPa)-Phosphorus(wt%)



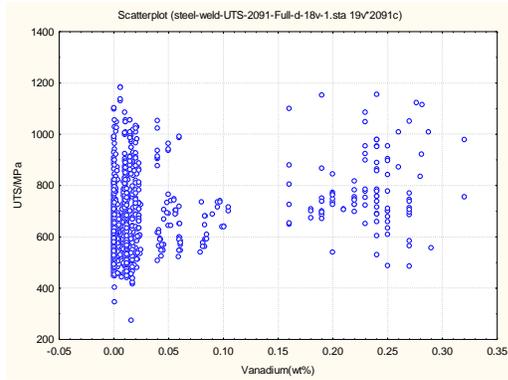
Ultimate Tensile Strength (MPa)-Nickel(wt%)



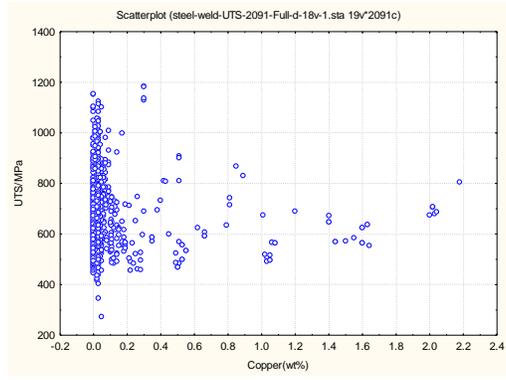
Ultimate Tensile Strength (MPa)-Chromium(wt%)



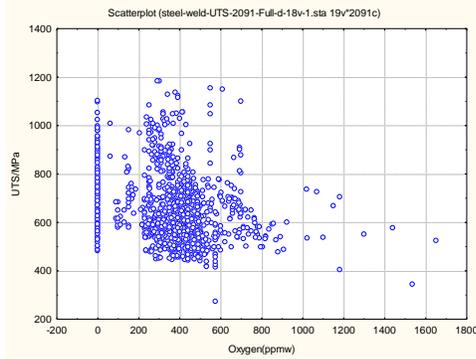
Ultimate Tensile Strength (MPa)-Molybdenum(wt%)



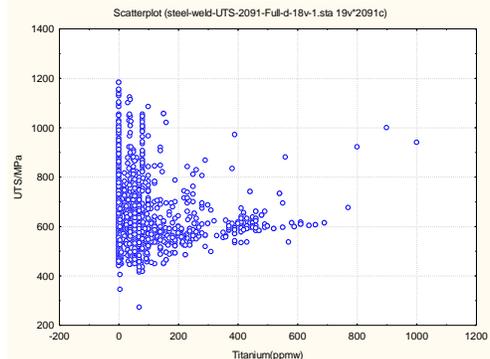
Ultimate Tensile Strength (MPa)-Vanadium(wt%)



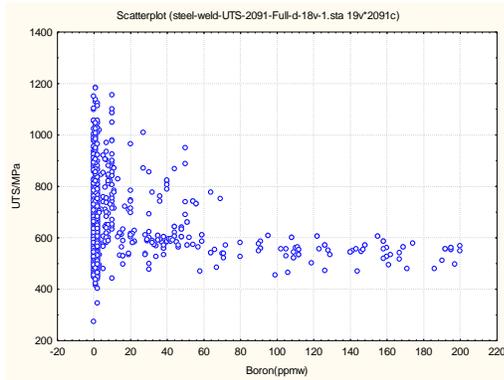
Ultimate Tensile Strength (MPa)-Copper(wt%)



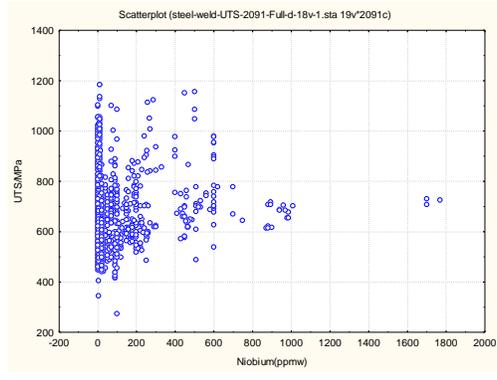
Ultimate Tensile Strength (MPa)-Oxygen(ppm)



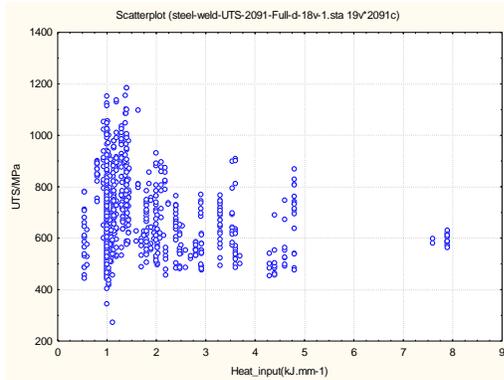
Ultimate Tensile Strength (MPa)-Titanium(ppm)



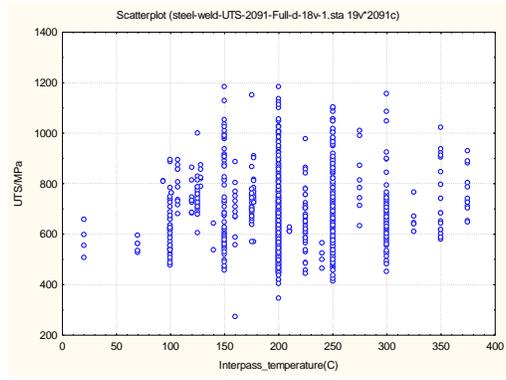
Ultimate Tensile Strength (MPa)-Boron(ppm)



Ultimate Tensile Strength (MPa)-Niobium(ppm)



Ultimate Tensile Strength (MPa)-Heat Input(KJ mm-1)



Ultimate Tensile Strength (MPa)-Interpass Temp(C)

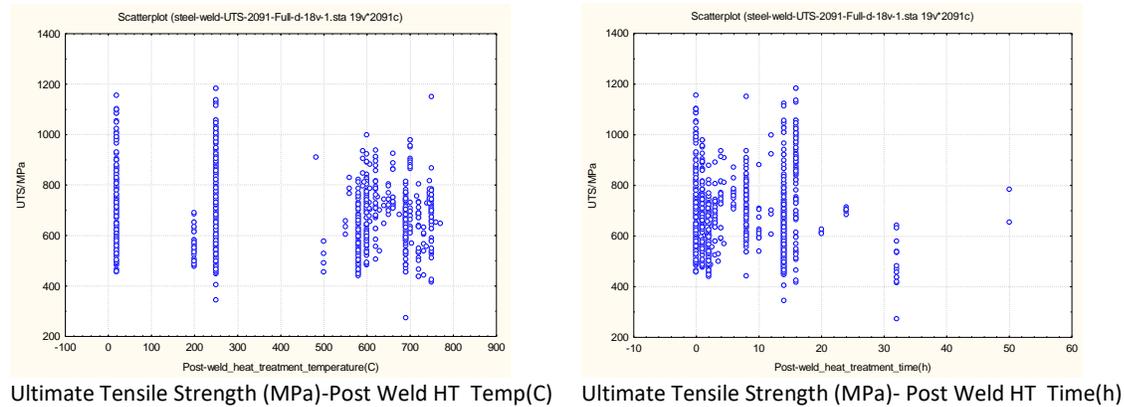


Figure 3.5 : Database distribution used for **Ultimate Tensile Strength** model. “p.p.m .’ corresponds to parts per million by weight.

3.2.2 Neural Network Models for Ultimate Tensile Strength

3.2.2.1 Bayesian Neural Network Model and procedure

- 1 Data of ultimate tensile strength were collected and plotted in the form of Scatter plots.
2. Data prepared according to the file format required to run in Neural Network Softwares.
(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)
3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)
4. Data of Ferritic Steel Weld’s Ultimate Tensile Strength 2091 run in NeuroMat Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.10

Neural network architecture for Bayesian Neural Network was set in NeuroMat Software :

Three layers : **Input Layer**(Input Variables), **Hidden Layer** (Algorithms) and **Output Layer** (Yield Strength)

Algorithms : Bigback 5

5. The data of Ferritic Steel Weld's Ultimate Tensile Strength 2091 run in NeuroMat Software with above Neural network architecture for best Neural Network Committee model. The best committee model was decided on the basis of smallest test error of the committee model.

6. For best committee model, the data of Ferritic Steel Weld's Ultimate Tensile Strength 2091 run in NeuroMat Software repeatedly hundred of times and finalise the best committee model with smallest test error. (NeuroMat gives in single run set of 100 models which required time in hours. Out of these 100 models, the models in the committee are selected on the basis of smallest test error. The number of models in committee varies everytime with repeatedly running the data in NeuroMat. Thus the selection of committee model with a smallest test error is time consuming.)

Some more than hundred ultimate tensile strength neural network models were trained on a training dataset which consisted of a random selection of 70% of the data 1464 from the ultimate tensile strength dataset. And 20% of the data 418 from ultimate tensile strength data set was used for cross validation. The remaining 209 data formed the test dataset which was used to see how the model generalizes on unseen data. Each model contained the 18 inputs listed in Table 1 but with different numbers of hidden units or the random seeds used to initiate the values of the weights. Fig. 3.6 shows the results. As expected, the perceived level of noise (σ_y) in the normalised ultimate tensile strength decreases as the number of hidden units increases, Fig. 3.6a. This is not the case for the test error, which goes through a minimum at sixteen hidden units, Fig. 3.6b, and for the log predictive error which reaches a maximum at seventeen hidden units, Fig. 3.6c.

The error bars presented throughout this work represent a combination of the perceived level of noise σ_y in the output and the fitting uncertainty estimated from the Bayesian framework. It is evident that there are a few outliers in the plot of the predicted versus measured ultimate tensile strength for the test dataset, Fig. 3.6f. Each of these outliers has been investigated and found to represent unique data which are not represented in the training dataset, Fig. 3.6e. It is possible

that a committee of models can make a more reliable prediction than an individual model (Chapter 2).

The best models are ranked using the values of the log predictive errors Fig. 3.6c. Committees are then formed by combining the predictions of the best L models, where $L = 1, 2, \dots$; the size of the committee is therefore given by the value of L . A plot of the test error of the committee versus its size gives a minimum which defines the optimum size of the committee, as shown in Fig. 3.6d. The test error associated with the best single model is clearly greater than that of any of the committees Fig. 3.6d. The committee with eight models was found to have an optimum membership with the smallest test error. The committee was therefore retrained on the entire data set without changing the complexity of any of its member models.

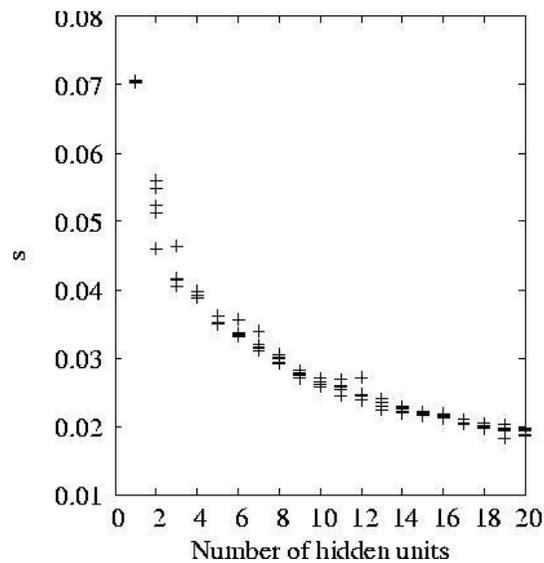


Figure 3. 6 (a) σ_y vs Hidden units

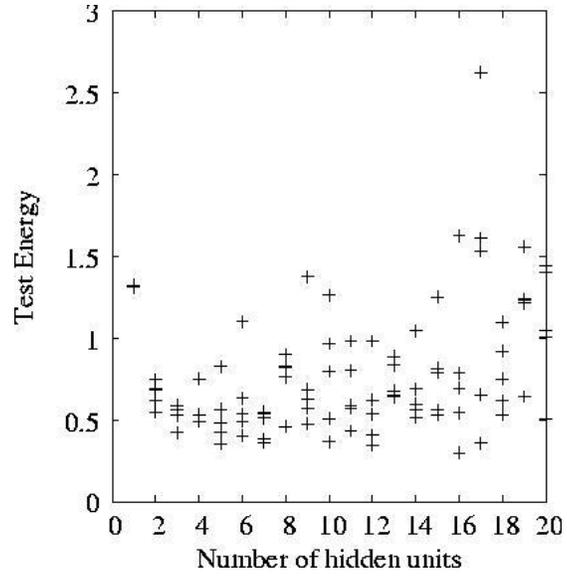


Figure 3. 6 (b) Test Error vs Hidden units.

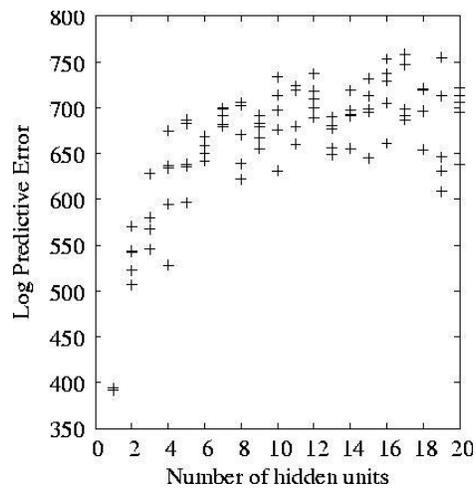


Figure 3. 6 (c) Log predictive error vs Hidden units

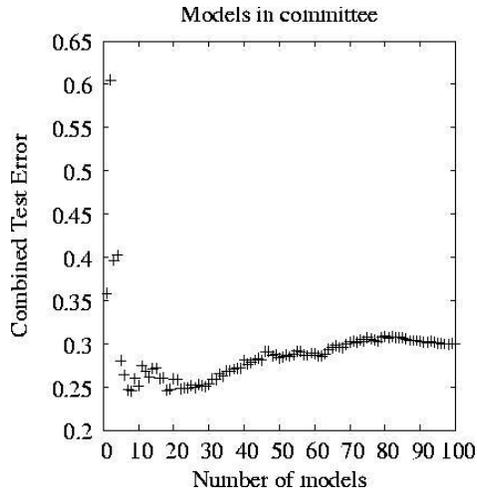


Figure 3.6 (d) Test Error vs Models in committee

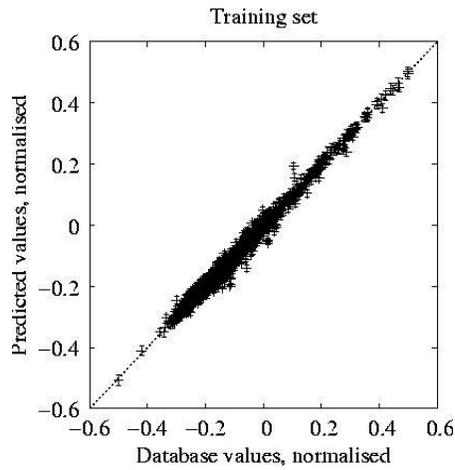


Figure 3.6 (e) Predicted normalized UTS. vs Measured normalized UTS. (Training Dataset)

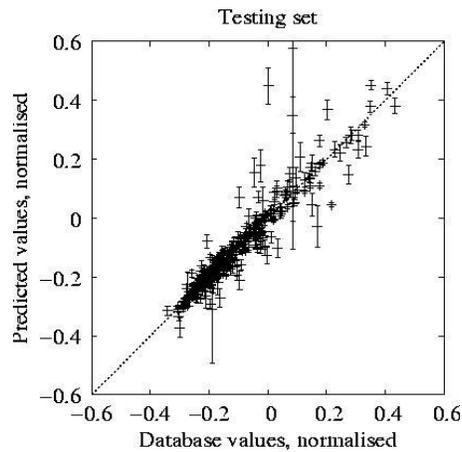


Figure 3.6 (f) Predicted normalized UTS. vs Measured normalized UTS. (Test Dataset)

Figure 3.6 . (a,b,c,d,e,f) **Ultimate Tensile Strength (UTS)** model features.

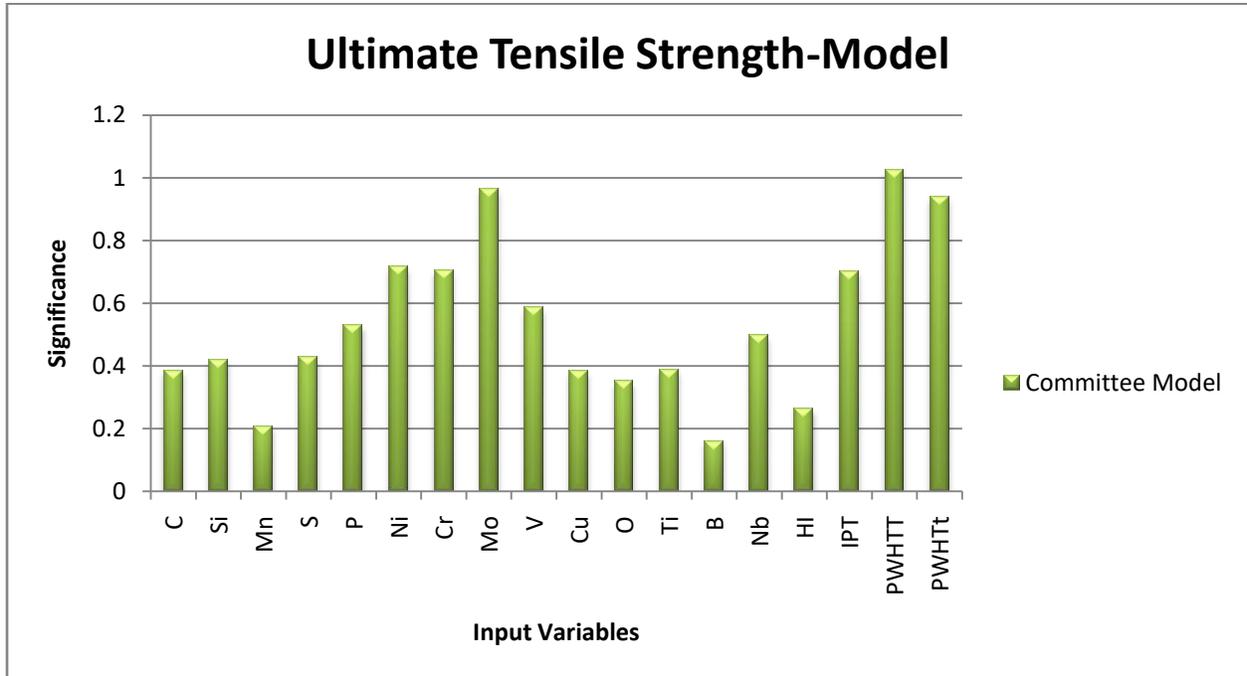


Figure 3.7 The perceived significance σ_w value of best eight **Ultimate Tensile Strength** models for each of the inputs.

Fig. 3.7 indicates the significance σ_w of each of the input variables, as perceived by first eight neural network models in the committee. The σ_w value represents the extent to which a particular input explains the variation in the output, rather like a particular correlation coefficient in linear regression analysis. The post-weld heat treatment temperature on the whole explains a large proportion of variation in the ultimate tensile strength Figure. 3.7. All variables considered are found to have a significant effect on the output indicating a good selection of inputs.

3.2.3 Comparison of Neural network models and procedure (MLP, RBF, GRNN)

1 Data of ultimate tensile strength were collected and plotted in the form of Scatter plots.

2. Data prepared according to the file format required to run in Neural Network Softwares.

(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)

3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)

4. Data of Ferritic Steel Weld's Ultimate Tensile Strength 2091 run in Statistica Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.11

Neural network architecture was set in Statistica software for MLP, RBF and GRNN :

MLP 17:17-10-1:1 Algorithms : BP100,CG20,CG18b

RBF 17:17-530-1:1 Algorithms : SS,KN,PI

GRNN 17:17-1061-2-1:1 Algorithms : SS

BP Back propagation, CG Conjugate gradient descent, SS (sub) sample, KN K-nearest neighbor (deviation assignment), PI Pseudo-invert (linear least squares), b Best network (the network with lowest selection error in the run was restored)

A neural network's architecture is of form I:N-N-N:O, where I is the number of input variable, O the number of output variables, N the number of units in each layer.

5. The data of Ferritic Steel Weld's Ultimate Tensile Strength 2091 run in Statistica Software with above Neural network architecture for best Neural Network model in all three MLP, RBF and GRNN.

6. For best model, the data of Ferritic Steel Weld's Ultimate Tensile Strength 2091 run in Statistica Software repeatedly hundred of times and finalise the best Neural Network model with smallest training error in all three MLP, RBF and GRNN.

7. The neural network model with the smallest training error was the GRNN model.

Table 3.5 shows the comparison of selected Neural Network models on the basis of their Training Errors. The GRNN models have lowest Training Errors for Ultimate Tensile Strength of Ferritic Steel Welds. The GRNN models are selected for modeling from three basic neural network methods (MLP, RBF, GRNN). Statistica 7.1 software is used for MLP, RBF and GRNN.

Table 3.5 Comparison of Neural network models (MLP, RBF, GRNN)

Ultimate Tensile Strength Models				
MLP	Train Error	Test Error	Training/Members	Remarks
MLP 18:18-12-1:1 (Model:No.3)	0.035736	0.044758	BP100,CG481b	1 H layer
MLP 18:18-13-7-1:1 (Model:No.8)	0.039741	0.060027	BP100,CG454b	2 H layer
MLP 18:18-13-8-10-1:1 (Model:No.6)	0.039139	0.046157	BP100,CG478b	3 H layer
Ultimate Tensile Strength Models				
RBF	Train Error	Test Error	Training/Members	Remarks
RBF 18:18-81-1:1 (Model:No.18)	0.002626	0.003150	SS,EX,PI	1 H layer
Ultimate Tensile Strength Models				
GRNN	Train Error	Test Error	Training/Members	Remarks
GRNN 18:18-1047-2-1:1 (Model:No.1)	0.000290	0.003402	SS	2 H layer
Note: See Appendix C for Profile String of Statistica Neural Network Software				

3.2.4 Best GRNN Model for Ultimate Tensile Strength

The normal behaviour of the Predicted Ultimate Tensile and Observed Ultimate Tensile Strength are observed in the Figure. 3.8 for Training data, Validation data and Testing data. Training of the model is excellent by GRNN method.

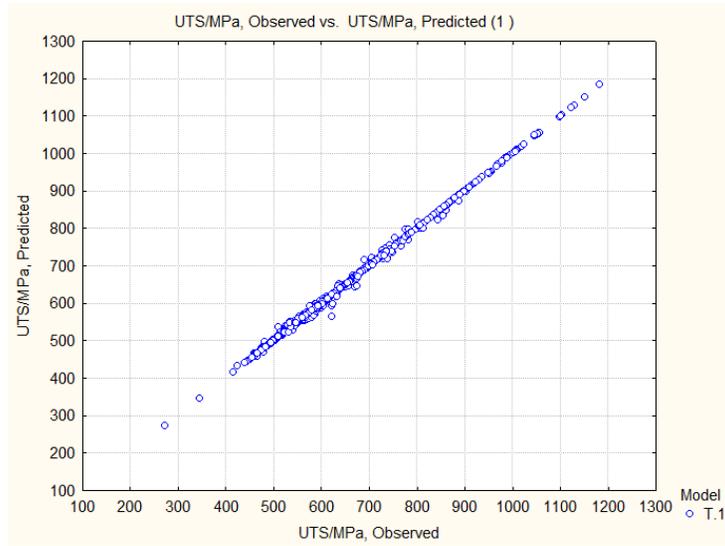


Figure a Training Data for GRNN model of Ultimate Tensile Strength

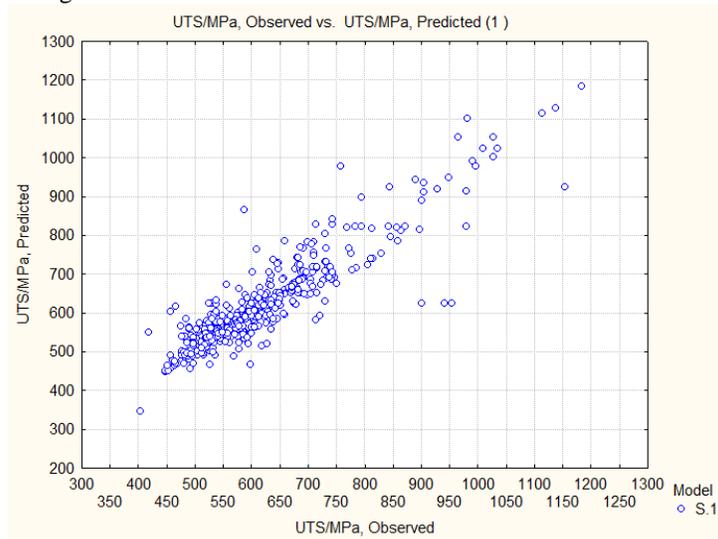


Fig b Validation Data for GRNN model of Ultimate Tensile Strength

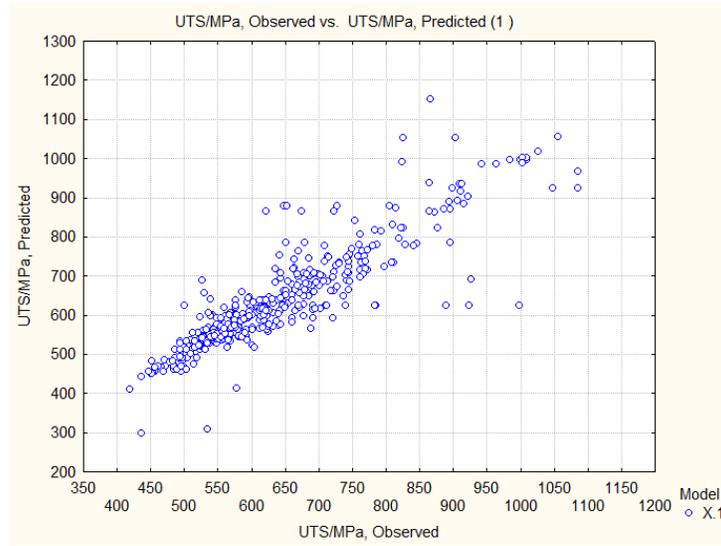


Fig c Test Data for GRNN model of Ultimate Tensile Strength

Figure 3.8 Training data, validation data and test data of the Best GRNN model for Ultimate tensile Strength.

The best model of GRNN has training error 0.000290, validation error (selection error) 0.003058, and testing error 0.003402. This model is used for getting the results in form of various response graphs to understand the trend between the input variables and output variable (Ultimate Tensile Strength).(Figure 4.5)

Table 3.6 Comparison of Significance of Best Trained Models of Ultimate Tensile Strength

Input Variables	Significance GRNN Model	Significance BNN Model
Carbon(wt%)	9	13
Silicon(wt%)	11	11
Manganese(wt%)	3	17
Sulphur(wt%)	16	10
Phosphorus(wt%)	17	8
Nickel(wt%)	1	4
Chromium(wt%)	6	5
Molybdenum(wt%)	4	2
Vanadium(wt%)	5	7
Copper(wt%)	14	14
Oxygen(ppm)	18	15
Titanium(ppm)	13	12
Boron(ppm)	15	18
Niobium(ppm)	8	9
Heat_input(kJ.mm-1)	12	16
Interpass_temperature(C)	7	6
Postweld_heat_treatment_temperature(C)	2	1
Post-weld_heat_treatment_time(h)	10	3

Table 3.6. shows the comparison of Significance of the GRNN and BNN models. Number 1 indicates highest value of significance and Number 18 lowest value of significance. Most of the Input Variables are closer in significance for both the models. All input variables considered are found to have a significant effect on the output indicating a good selection of inputs.

3.2.5 Neural Network and Genetic Algorithms Modeling for Ultimate Tensile Strength of Ferritic Steel Welds

3.2.5.1 Genetic Algorithms parameters and procedure

A genetic algorithm has been developed in language C considering the following parameters:

Number of populations = 3

Number of generations = 3000

Population size = 20 chromosomes

When a new generation is created, the following steps are followed: after ranking the 20 chromosomes according to their scores, the first chromosome is copied without change. The chromosomes 2 to **19** are recombined with each others. One gene of one of these chromosomes is mutated between $\pm 0.2\%$. The chromosome 20, with the worst score, is killed and a new random chromosome is generated and incorporated in the new population.

This program can calculate the best set (x_1, x_2, \dots, x_j) of input parameters for a desired output y , which is in this study, the Ultimate Tensile Strength of ferritic steel welds, for which a Bayesian neural network model was developed[32].

The steps for Genetic Algorithms Modelling:

- First, all the files related to the neural network created for the ultimate tensile strength were put in the folder "gacode" to optimise. These files were the following:

```
generate44.exe  
norm_test.in  
_w*f  
*.lu  
spec1.tl  
outran.x  
MINMAX
```

- Then, the labels of the inputs variables of the neural network were written in the "labels.tct" file
- Then the all inputs variables were define in the "values" file to vary.
- Then, the desired target value of ultimate tensile strength was normalised and entered it in the "nninput" file, as well as the wanted accuracy.
- Finally, the C program "ga_code" was compiled and executed.

After execution of the Genetic Algorithms program, the output was the values of 18 input variables for given target value of the ultimate tensile strength of Ferritic Steel Weld. The calculation time was in hours.

Three different target values of Ferritic Steel Weld's ultimate tensile strength were taken and Genetic Algorithms programs were run. The outputs were given in result and discussion Chapter 4.

3.3 Elongation Models

3.3.1 Experimental Data base

All of the data collected are from multi runweld deposits in which the joint is designed to minimize dilution from the base metal, to enable specifically the measurement of all weld metal properties. Furthermore, they all represent electric arc welds made using one of the following processes: manual metal arc (MMAW), submerged arc welding (SAW) and tungsten inert gas (TIG). The welding process itself was represented only by the level of heat input. This is because a large number of published papers did not specify welding parameters in sufficient detail to enable the creation of a dataset without missing values. Missing values cannot be tolerated in the method used here. If the effect of a welding process is not properly represented by the heat input and chemical composition, then neglect of any important parameters will make the predictions more 'noisy'. As discussed below, the noise in the output was found to be acceptable; a greater uncertainty arises from the lack of a uniform coverage of the input space. The data were collected from a large number of sources [33] to [76].

The aim of the neural network analysis was to predict the Elongation as a function of a large number of variables, including the chemical composition, the welding heat input and any heat treatment. The Elongation database consists of 1827 separate experiments. Neural network methods used in this work cannot cope with missing values of any of the variables.

3.3.1.1 Elongation Database

Table 3.7 shows the range, mean and standard deviation of each variable including the output (elongation). The purpose here is simply to list the variables and provide an idea of the range covered. It is emphasized however, that unlike linear regression analysis, the information in Table 3.7 cannot be used to define the range of applicability of the neural network model. This is because the inputs are in general expected to interact. We shall see later that it is the Bayesian framework of our neural network analysis which allows the calculation of error bars which define the range of useful applicability of the trained network. A visual impression of the spread

of data is shown in Fig. 3.9. It can be concluded from from Figure. 4.7(a to r) and Figure. 4.8(a to r) that the effect of Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Oxygen, Titanium, Boron, Niobium, Heat_input, Interpass_temperature, Post- weld heat treatment temperature and Post-weld heat treatment time on the Elongation of Ferritic Steel Welds have been systematically studied by BNN and GRNN.[28]

It can be concluded from Figure. 4.9.1 to 4.9.13 that the effect in combination of any two input variables (Independent variables) from Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Oxygen, Titanium, Boron, Niobium, Heat input, Interpass temperature, Post- weld heat treatment temperature and Post-weld heat treatment time on the Elongation of Ferritic Steel Welds have been systematically studied by GRNN.

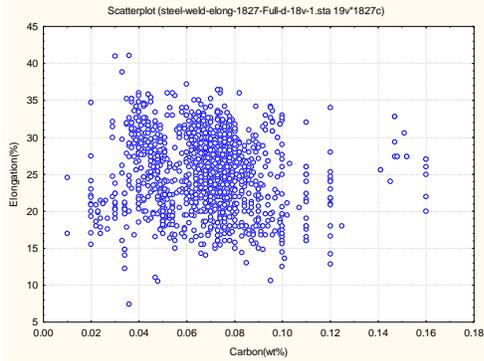
The prediction of the all Input variables for Targeted Elongation by Genetic Algorithms is given in Table 4.8. These can be useful for the design of the Ferritic Steel Welds. Genetic Algorithms can design the Ferritic Steel Welds by extrapolation beyond the existing data.

Table 3.7 shows the range, mean and standard deviation of each variable including the output (Elongation).

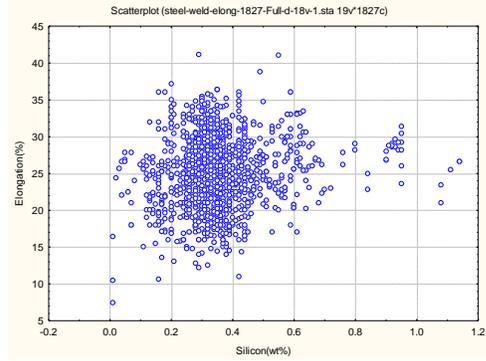
Table 3.7 The Input Variables for **Elongation** Model. “p.p.m .’ corresponds to parts per million by weight.

Variables	Min	Max	Average	StDev
C wt%	0.01	0.16	0.0688	0.0189
Si wt%	0.01	1.14	0.352	0.1229
Mn wt%	0.24	2.31	1.2102	0.3986
S wt%	0.002	0.14	0.0078	0.0049
P wt%	0.001	0.25	0.0101	0.0071
Ni wt%	0	10.66	0.5374	1.5246
Cr wt%	0	9.35	0.4452	1.1844
Mo wt%	0	2.4	0.1798	0.3569
V wt%	0	0.32	0.0151	0.0437
Cu wt%	0	2.04	0.0628	0.202
O ppm	63	1650	411.2567	117.9406
Ti ppm	0	1000	84.9978	126.1291
B ppm	0	200	10.306	29.8403
Nb ppm	0	1770	47.0246	139.0368
HI kJ mm-1	0.55	4.8	1.2294	0.7057
IPT C	20	350	203.8697	35.2603
PWHTT C	20	750	319.5599	188.6206
PWHTT h	0	32	10.3452	6.1765
Elongation %	7.4	41.1	25.6466	4.6985

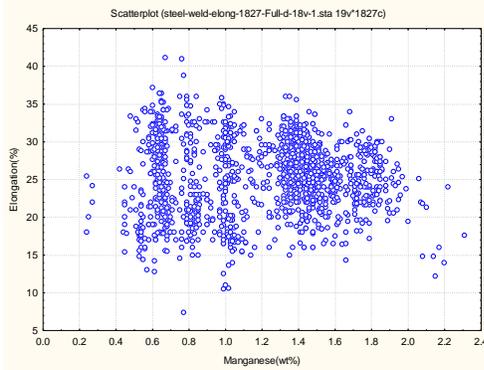
Scatter Plots of Elongation- Data-1827



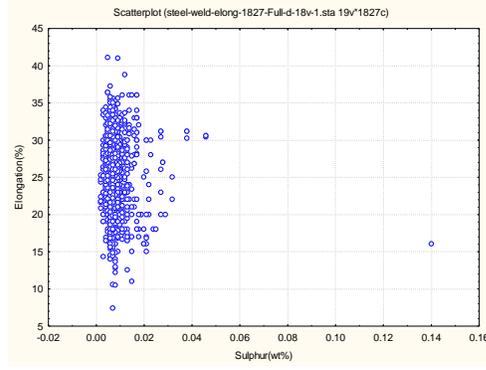
Elongation % - Carbon (wt%)



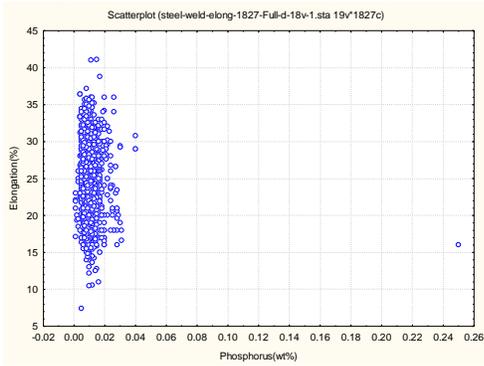
Elongation % - Silicon (wt%)



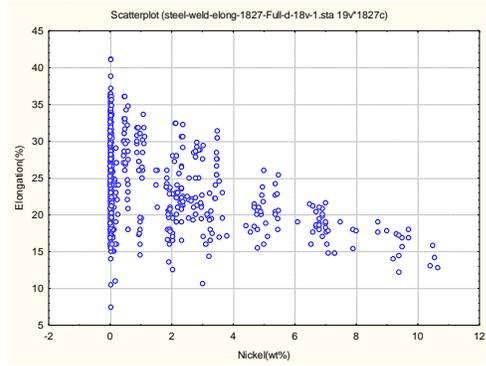
Elongation % - Manganese (wt%)



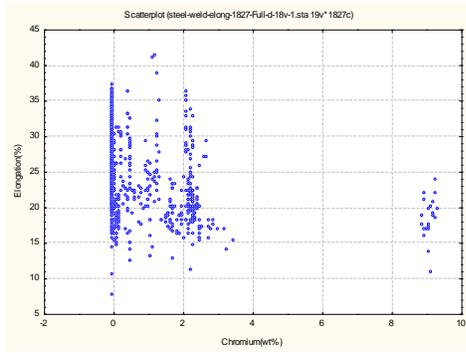
Elongation % - Sulphur (wt%)



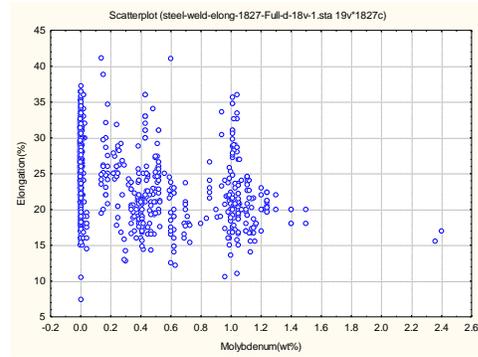
Elongation % - Phosphorus (wt%)



Elongation % - Nickel (wt%)

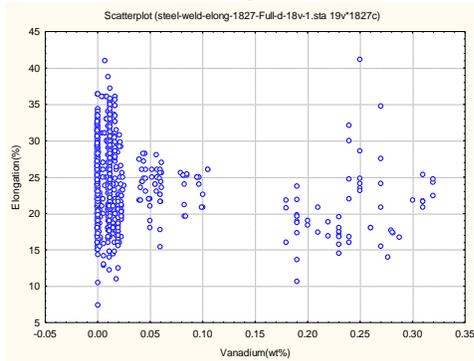


Elongation % - Chromium (wt%)

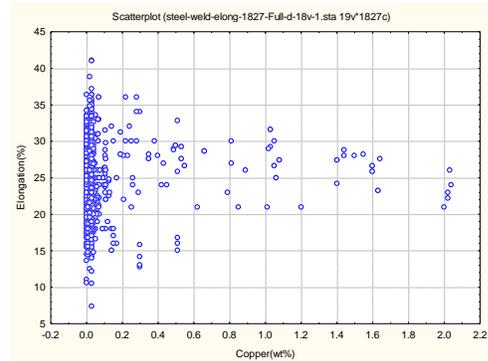


Elongation % - Molybdenum (wt%)

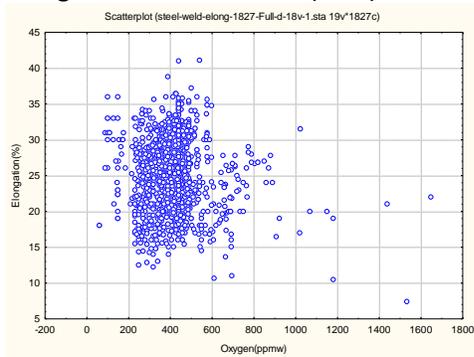
Scatter Plots of Elongation- Data-1827



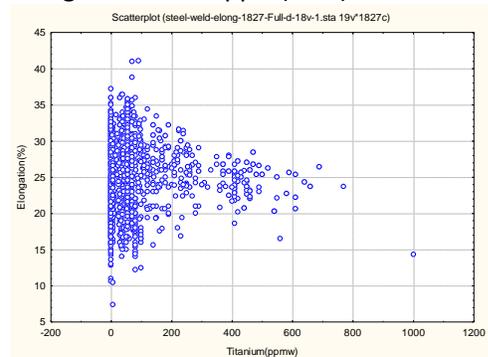
Elongation % - Vanadium (wt%)



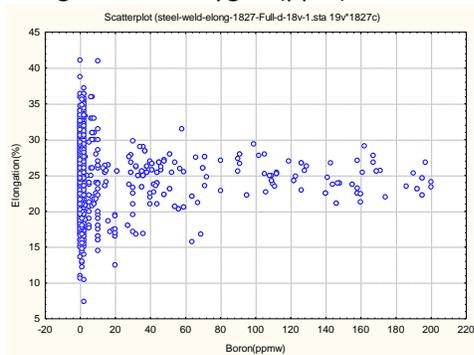
Elongation % - Copper(wt%)



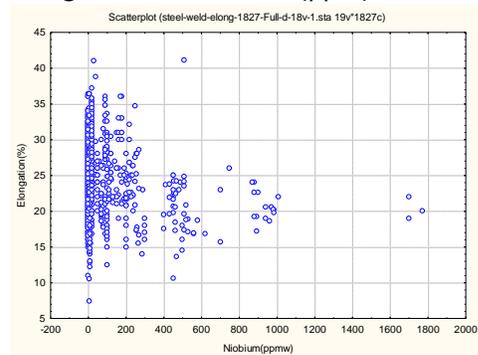
Elongation % - Oxygen (ppm)



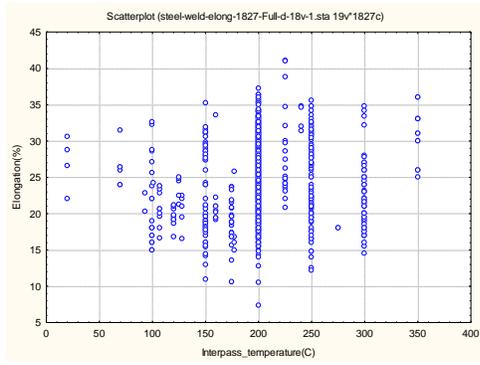
Elongation % - Titanium (ppm)



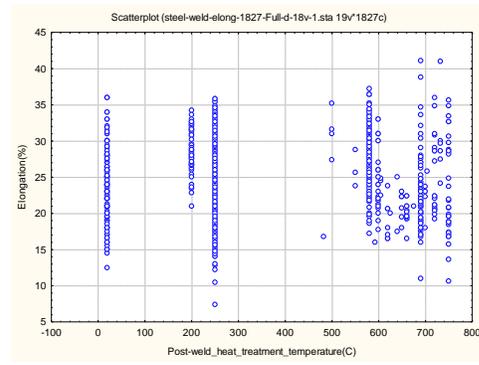
Elongation % - Boron (ppm)



Elongation % - Niobium(ppm)

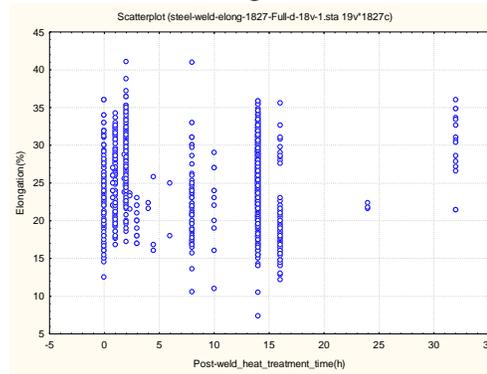


Elongation % - Interpass Temp(C)



Elongation % - Postweld Heat Treatment Temp (C)

Scatter Plots of Elongation- Data-1827



Elongation % - Postweld Heat Treatment Time (h)

Figure 3.9 : Database distribution used for **Elongation** model. “p.p.m .’ corresponds to parts per million by weight.

3.3.2 Neural Network Models for Elongation

3.3.2.1 Bayesian Neural Network Model and procedure

1 Data of elongation were collected and plotted in the form of Scatter plots.

2. Data prepared according to the file format required to run in Neural Network Softwares.

(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)

3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)

4. Data of Ferritic Steel Weld's Elongation 1827 run in NeuroMat Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.10

Neural network architecture for Bayesian Neural Network was set in NeuroMat Software :

Three layers : **Input Layer**(Input Variables), **Hidden Layer** (Algorithms) and **Output Layer** (Yield Strength)

Algorithms : Bigback 5

5. The data of Ferritic Steel Weld's Elongation 1827 run in NeuroMat Software with above Neural network architecture for best Neural Network Committee model. The best committee model was decided on the basis of smallest test error of the committee model.

6. For best committee model, the data of Ferritic Steel Weld's Elongation 1827 run in NeuroMat Software repeatedly hundred of times and finalise the best committee model with smallest test error. (NeuroMat gives in single run set of 100 models which required time in hours. Out of these 100 models, the models in the committee are selected on the basis of smallest test error. The number of models in committee varies everytime with repeatedly running the data in NeuroMat. Thus the selection of committee model with a smallest test error is time consuming.)

Some more than hundred elongation neural network models were trained on a training dataset which consisted of a random selection of 70%of the data 1279 from the ultimate tensile strength

dataset. And 20% of the data 365 from ultimate tensile strength data set was used for cross validation. The remaining 183 data formed the test dataset which was used to see how the model generalizes on unseen data. Each model contained the 18 inputs listed in Table 3.7 but with different numbers of hidden units or the random seeds used to initiate the values of the weights. Fig. 3.10 shows the results. As expected, the perceived level of noise (σ_y) in the normalised ultimate tensile strength decreases as the number of hidden units increases, Fig. 3.10a. This is not the case for the test error, which goes through a minimum at six hidden units, Fig. 3.10b, and for the log predictive error which reaches a maximum at twelve hidden units, Fig. 3.10c.

The error bars presented throughout this work represent a combination of the perceived level of noise σ_y in the output and the fitting uncertainty estimated from the Bayesian framework. It is evident that there are a few outliers in the plot of the predicted versus measured Elongation for the test dataset, Fig. 3.10f. Each of these outliers has been investigated and found to represent unique data which are not represented in the training dataset, Fig. 3.10e.

It is possible that a committee of models can make a more reliable prediction than an individual model (Chapter 2). The best models are ranked using the values of the log predictive errors Fig. 3.10c. Committees are then formed by combining the predictions of the best L models, where $L = 1, 2, \dots$; the size of the committee is therefore given by the value of L . A plot of the test error of the committee versus its size gives a minimum which defines the optimum size of the committee, as shown in Fig. 3.10d.

The test error associated with the best single model is clearly greater than that of any of the committees Fig. 3.10d. The committee with two models was found to have an optimum membership with the smallest test error. The committee was therefore retrained on the entire data set without changing the complexity of any of its member models.

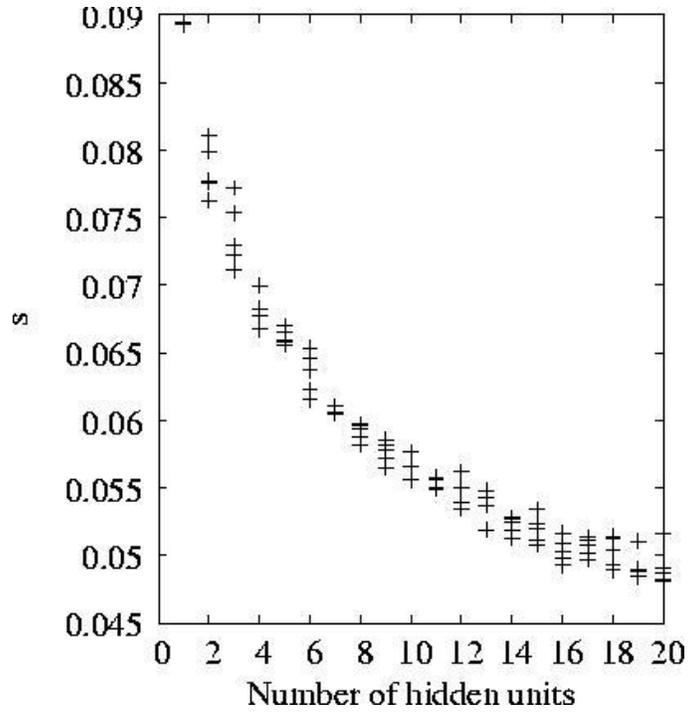


Figure 3.10 (a) σy vs Hidden units

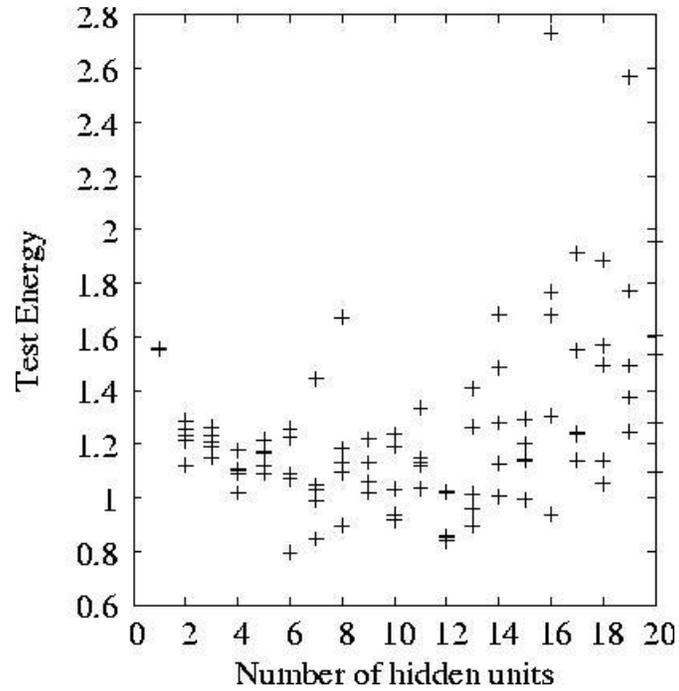


Figure 3.10 (b) Test Error vs Hidden units.

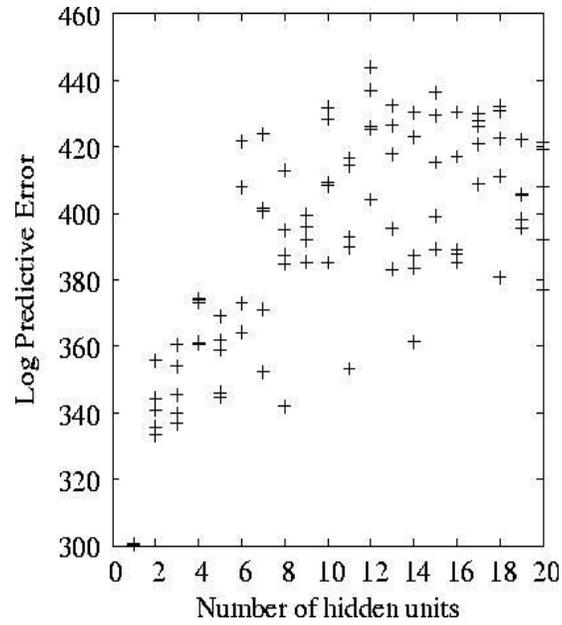


Figure 3.10 (c) **Log predictive error vs Hidden units**

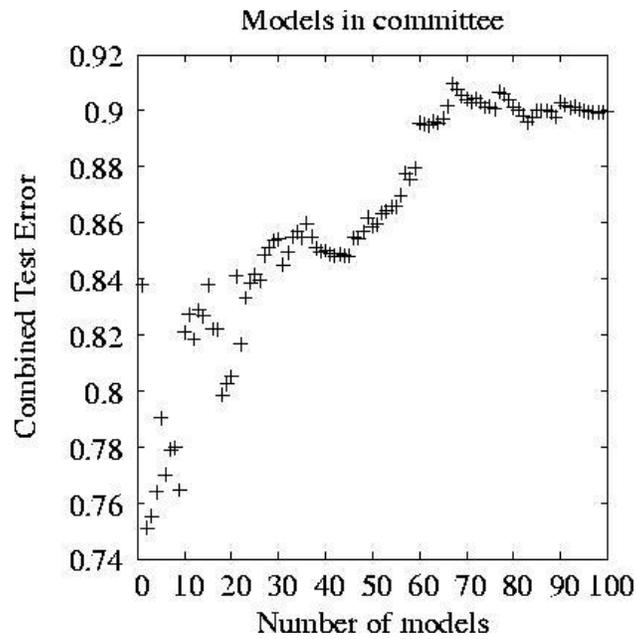


Figure 3.10 (d) **Test Error vs Models in committee**

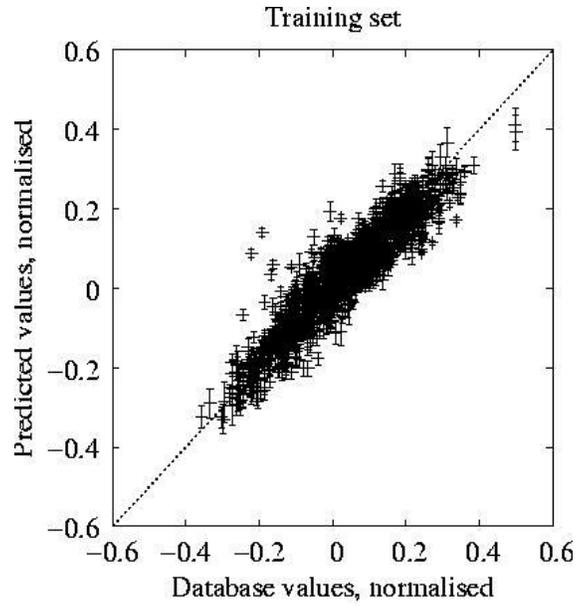


Figure 3.10 (e) **Predicted normalized EL. vs Measured normalized EL. (Training Dataset)**

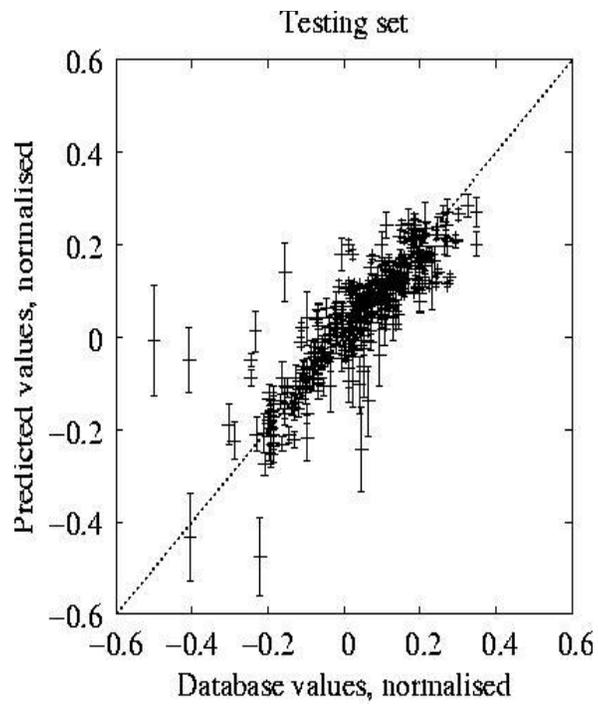


Figure 3.10 (f) **Predicted normalized EL. vs Measured normalized EL. (Test Dataset)**

Figure 3.10 (a,b,c,d,e,f) **Elongation (EL) model features.**

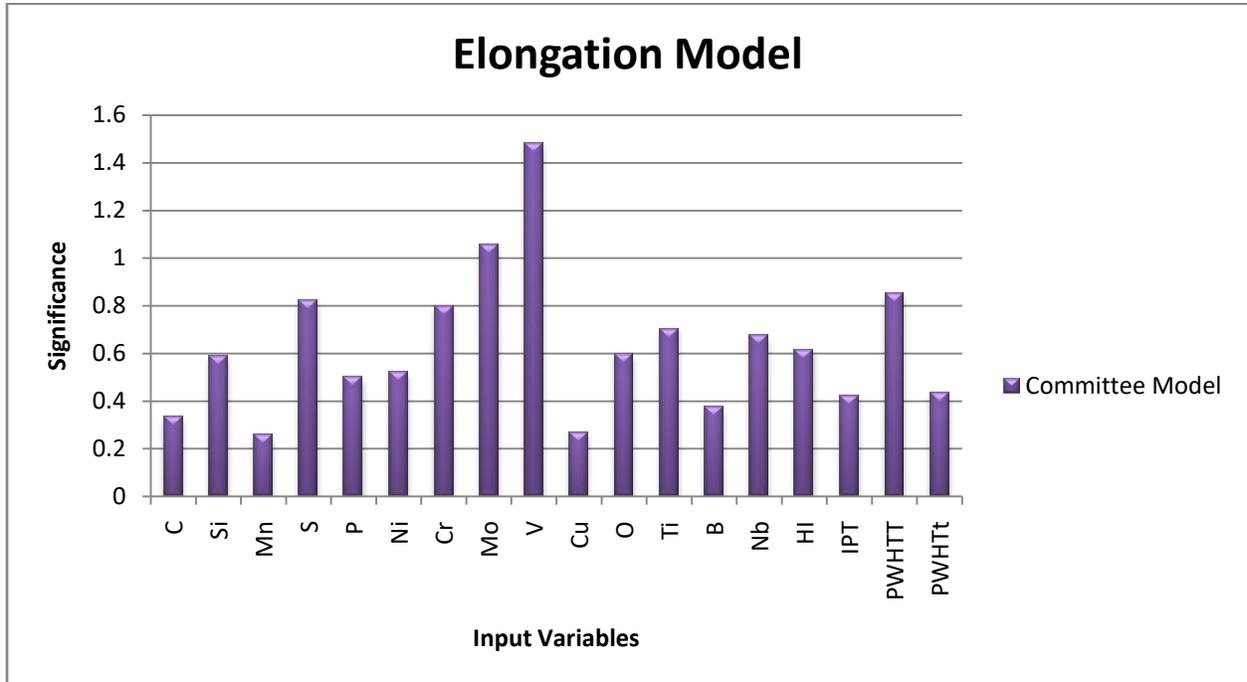


Figure 3.11 The perceived significance σ_w value of best two **Elongation** models for each of the inputs.

Fig. 3.11 indicates the significance σ_w of each of the input variables, as perceived by first Two neural network models in the committee. The σ_w value represents the extent to which a particular input explains the variation in the output, rather like a particular correlation coefficient in linear regression analysis. The Vanadium on the whole explains a large proportion of variation in the Elongation Figure. 3.11. All variables considered are found to have a significant effect on the output indicating a good choice of inputs.

3.3.3 Comparison of Neural network models and procedure (MLP, RBF, GRNN)

1 Data of elongation were collected and plotted in the form of Scatter plots.

2. Data prepared according to the file format required to run in Neural Network Softwares.

(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)

3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)

4. Data of Ferritic Steel Weld's Elongation 1827 run in Statistica Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.11

Neural network architecture was set in Statistica software for MLP, RBF and GRNN :

MLP 17:17-10-1:1 Algorithms : BP100,CG20,CG18b

RBF 17:17-530-1:1 Algorithms : SS,KN,PI

GRNN 17:17-1061-2-1:1 Algorithms : SS

BP Back propagation, CG Conjugate gradient descent, SS (sub) sample, KN K-nearest neighbor (deviation assignment), PI Pseudo-invert (linear least squares), b Best network (the network with lowest selection error in the run was restored)

A neural network's architecture is of form I:N-N-N:O, where I is the number of input variable, O the number of output variables, N the number of units in each layer.

5. The data of Ferritic Steel Weld's Elongation 1827 run in Statistica Software with above Neural network architecture for best Neural Network model in all three MLP, RBF and GRNN.

6. For best model, the data of Ferritic Steel Weld's Elongation 1827 run in Statistica Software repeatedly hundred of times and finalise the best Neural Network model with smallest training error in all three MLP, RBF and GRNN.

7. The neural network model with the smallest training error was the GRNN model.

Table 3.8 shows the comparison of selected Neural Network models on the basis of their Training Errors. The GRNN models have lowest Training Errors for Elongation of Ferritic Steel Welds. The GRNN models are selected for modeling from three basic neural network methods (MLP, RBF, GRNN).). Statistica 7.1 software is used for MLP, RBF and GRNN.

Table 3.8 Comparison of Neural network models (MLP, RBF, GRNN)

Elongation Models				
MLP	Train Error	Test Error	Training/Members	Remarks
MLP 18:18-15-10-5-1:1 (Model:No.11)	0.056027	0.071757	BP100,CG462b	3 H layers
MLP 18:18-29-1:1 (Model:No.11)	0.05845	0.076457	BP100,CG498b	1 H layer
MLP 18:18-8-1:1 (Model:No.43)	0.056123	0.191787	DD100,LM187b	1 H layer
MLP 18:18-11-7-1:1 (Model:No.15)	0.061902	0.077359	BP100,CG475b	2 H layer
Elongation Models				
RBF	Train Error	Test Error	Training/Members	Remarks
RBF 18:18-193-1:1 (Model:No.46)	0.0787	0.1125	SS,EX,PI	1 H layer
Elongation Models				
GRNN	Train Error	Test Error	Training/Members	Remarks
GRNN 18:18-915-2-1:1 (Model:No.01)	0.010208	0.123726	SS	2 H layer
Note: See Appendix C for Profile String of Statistica Neural Network Software				

3.3.4 Best GRNN Model for Elongation

The normal behaviour of the Predicted Elongation and Observed Elongation are observed in the Figure. 3.12 for Training data, Validation data and Testing data. Training of the model is excellent by GRNN method.

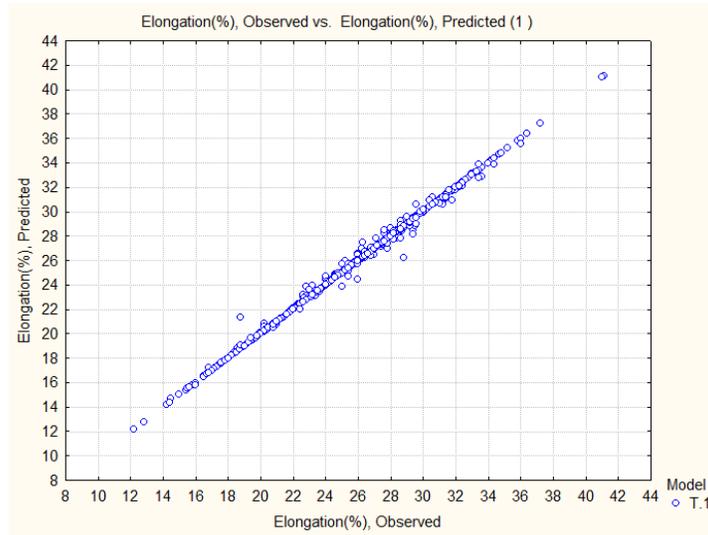


Figure a Training Data for GRNN model of Elongation

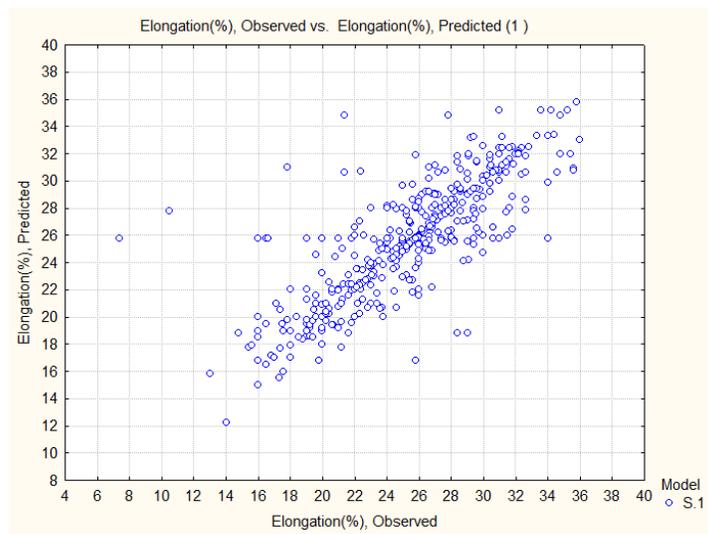


Fig b Validation Data for GRNN model of Elongation

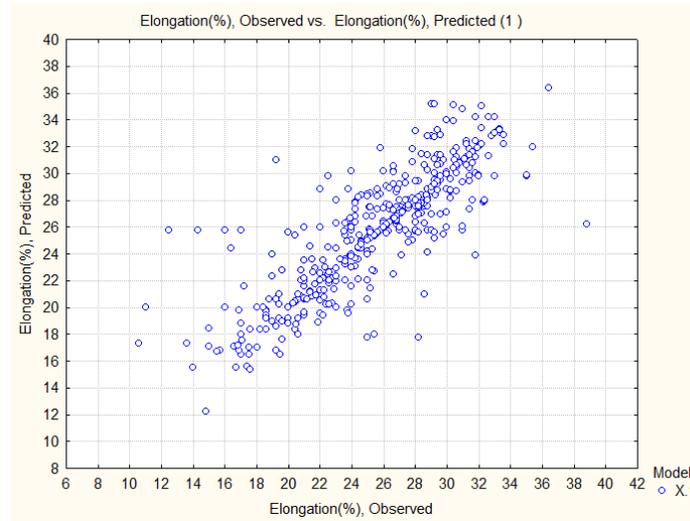


Fig c Test Data for GRNN model of Elongation

Figure 3.12 Training data, validation data and test data of the Best GRNN model for Elongation

The best model of GRNN has training error 0.010208, validation error (selection error) 0.134319 and testing error 0.123726. This model is used for getting the results in form of various response graphs to understand the trend between the input variables and output variable (Elongation). (Figure 4.8)

Table 3.9. Comparison of Significance of Best Trained Models of Elongation

Input Variables	Significance GRNN Model	Significance BNN Model
Carbon(wt%)	7	16
Silicon(wt%)	12	10
Manganese(wt%)	2	18
Sulphur(wt%)	17	4
Phosphorus(wt%)	15	12
Nickel(wt%)	1	11
Chromium(wt%)	3	5
Molybdenum(wt%)	6	2
Vanadium(wt%)	11	1
Copper(wt%)	18	17
Oxygen(ppm)	16	9
Titanium(ppm)	5	6
Boron(ppm)	13	15
Niobium(ppm)	8	7
Heat_input(kJ.mm-1)	10	8
Interpass_temperature(C)	9	14
Postweld_heat_treatment_temperature(C)	4	3
Post-weld_heat_treatment_time(h)	14	13

Table 3.9 shows the comparison of Significance of the GRNN and BNN models. Number 1 indicates highest value of significance and Number 18 lowest value of significance. Most of the Input Variables are closer in significance for both the models. All input variables considered are found to have a significant effect on the output indicating a good selection of inputs.

3.3.5 Neural Network and Genetic Algorithms Modeling for Elongation of Ferritic Steel Welds

3.3.5.1 Genetic Algorithms parameters and procedure

A genetic algorithm has been developed in language C considering the following parameters:

Number of populations = 3

Number of generations = 3000

Population size = 20 chromosomes

When a new generation is created, the following steps are followed: after ranking the 20 chromosomes according to their scores, the first chromosome is copied without change. The chromosomes 2 to 19 are recombined with each others. One gene of one of these chromosomes is mutated between $\pm 0.2\%$. The chromosome 20, with the worst score, is killed and a new random chromosome is generated and incorporated in the new population.

This program can calculate the best set (x_1, x_2, \dots, x_j) of input parameters for a desired output y , which is in this study, the elongation of ferritic steel welds, for which a Bayesian neural network model was developed[32].

The steps for Genetic Algorithms Modelling:

- First, all the files related to the neural network created for the elongation were put in the folder "gacode" to optimise. These files were the following:

```
generate44.exe  
norm_test.in  
_w*f  
*.lu  
specl.tl  
outran.x  
MINMAX
```

- Then, the labels of the inputs variables of the neural network were written in the "labels.tct" file
- Then the all inputs variables were define in the "values" file to vary.
- Then, the desired target value of elongation was normalised and entered it in the "nninput" file, as well as the wanted accuracy.

- Finally, the C program "ga_code" was compiled and executed.

After execution of the Genetic Algorithms program, the output was the values of 18 input variables for given target value of the elongation of Ferritic Steel Weld. The calculation time was in hours.

Three different target values of Ferritic Steel Weld's elongation were taken and Genetic Algorithms programs were run. The outputs were given in result and discussion Chapter 4.

3.4 Charpy Toughness Models

3.4.1 Experimental Data base

All of the data collected are from multi run weld deposits in which the joint is designed to minimize dilution from the base metal, to enable specifically the measurement of all weld metal properties. Furthermore, they all represent electric arc welds made using one of the following processes: manual metal arc (MMAW), submerged arc welding (SAW) and tungsten inert gas (TIG). The welding process itself was represented only by the level of heat input. This is because a large number of published papers did not specify welding parameters in sufficient detail to enable the creation of a dataset without missing values. Missing values cannot be tolerated in the method used here. If the effect of a welding process is not properly represented by the heat input and chemical composition, then neglect of any important parameters will make the predictions more 'noisy'. As discussed below, the noise in the output was found to be acceptable; a greater uncertainty arises from the lack of a uniform coverage of the input space. The data were collected from a large number of sources [33] to [76].

The aim of the neural network analysis was to predict the Charpy Toughness as a function of a large number of variables, including the chemical composition, the welding heat input and any heat treatment. The Charpy Toughness database consists of 3449 separate experiments. Neural network methods used in this work cannot cope with missing values of any of the variables.

3.4.1.1 Charpy Toughness Database

Table 3.10 shows the range, mean and standard deviation of each variable including the output (charpy toughness). The purpose here is simply to list the variables and provide an idea of the range covered. It is emphasized however, that unlike linear

regression analysis, the information in Table 3.10 cannot be used to define the range of applicability of the neural network model. This is because the inputs are in general expected to interact. We shall see later that it is the Bayesian framework of our neural network analysis which allows the calculation of error bars which define the range of useful applicability of the trained network. A visual impression of the spread of data is shown in Fig. 3.13. It can be concluded from Figure. 4.10 (a to t) and Figure. 4.11(a to t) that the effect of Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Oxygen, Titanium, Nitrogen, Boron, Niobium, Heat input, Interpass temperature, Post- weld heat treatment temperature, Post-weld heat treatment time and Testing Temperature Charpy Toughness on the Charpy Toughness of Ferritic Steel Welds have been systematically studied by BNN and GRNN.[28]

It can be concluded from Figure.4.12.1 to 4.12.18 that the effect in combination of any two input variables (Independent variables) from Carbon, Silicon, Manganese, Sulphur, Phosphorus, Nickel, Chromium, Molybdenum, Vanadium, Copper, Oxygen, Titanium, Nitrogen, Boron, Niobium, Heat input, Interpass temperature, Post- weld heat treatment temperature, Post-weld heat treatment time and Testing Temperature Charpy Toughness on the Charpy Toughness of Ferritic Steel Welds have been systematically studied by GRNN.

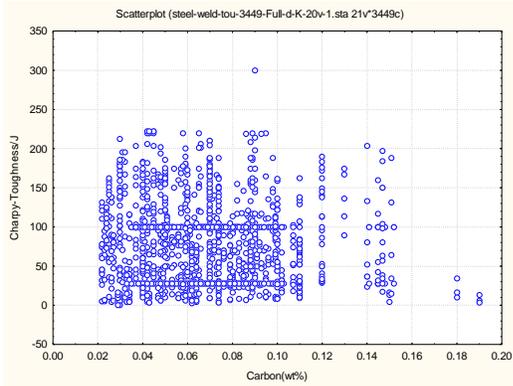
The predictions of the all Input variables for Targeted Charpy Toughness by Genetic Algorithms are given in Table 4.13. These can be useful for the design of the Ferritic Steel Welds. Genetic Algorithms can design the Ferritic Steel Welds by extrapolation beyond the existing data.

Table 3.10 shows the range, mean and standard deviation of each variable including the output (Charpy Toughness).

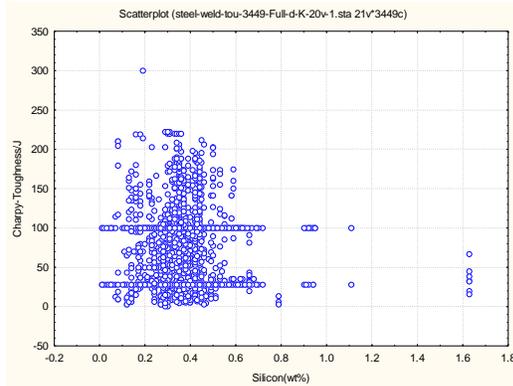
Table 3.10 The Input Variables for **Charpy Toughness** Model. “p.p.m .’ corresponds to parts per million by weight.

Variables	Min	Max	Average	StDev
C wt%	0.022	0.19	0.0692	0.0207
Si wt%	0.01	1.63	0.3527	0.1214
Mn wt%	0.23	2.31	1.2209	0.4446
S wt%	0.002	0.14	0.0078	0.0075
P wt%	0.003	0.25	0.0101	0.0128
Ni wt%	0	10.8	0.9933	2.26
Cr wt%	0	11.78	0.4406	1.323
Mo wt%	0	1.54	0.1818	0.3341
V wt%	0	0.53	0.0139	0.0404
Cu wt%	0	2.18	0.0638	0.2128
O ppm	63	1535	399.6638	110.6312
Ti ppm	0	770	96.0337	132.9401
N ppm	0	979	77.5725	60.8648
B ppm	0	200	13.1739	33.4533
Nb ppm	0	1770	37.6917	133.0933
HI kJ mm-1	0.6	6.6	1.1954	0.6596
IPT C	20	350	199.0003	31.0232
PWHTT C	0	760	186.1773	249.8889
PWHTt h	0	100	3.3429	6.6257
TTCT K	77	409	227.8425	38.3343
Charpy Toughness J	0	300	72.714	42.8411

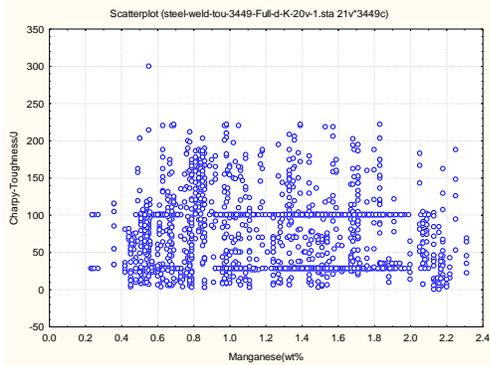
Scatter Plots of Toughness-Data-3449



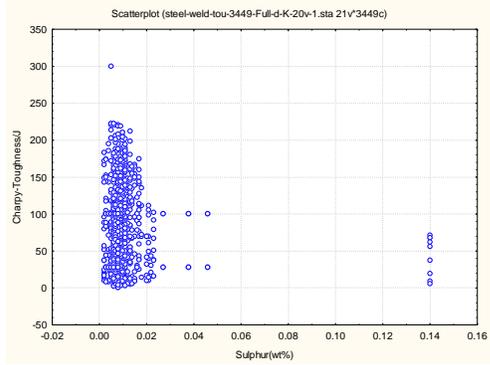
Toughness(J)-Carbon (wt%)



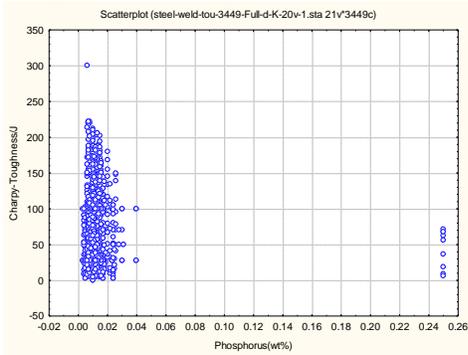
Toughness(J)-Silicon (wt%)



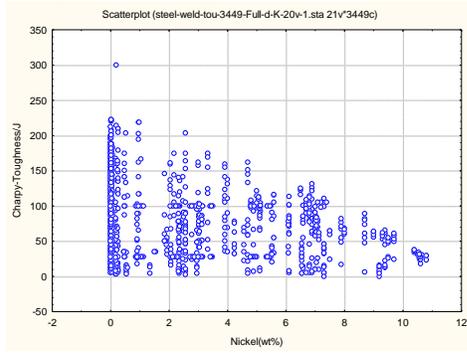
Toughness(J)-Manganese (wt%)



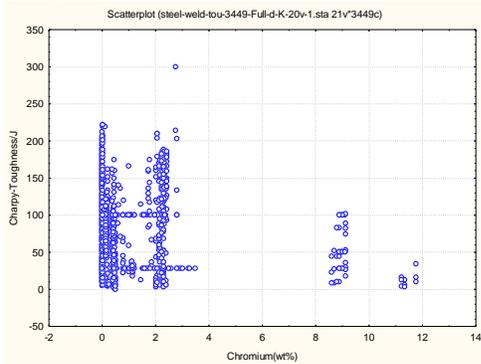
Toughness(J)-Sulphur (wt%)



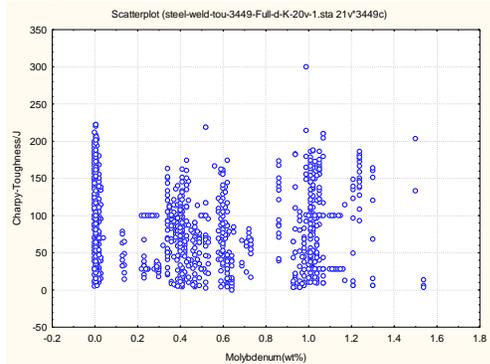
Toughness(J)-Phosphorus (wt%)



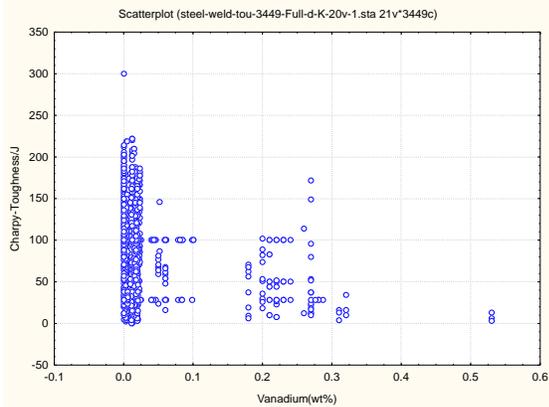
Toughness(J)-Nickel (wt%)



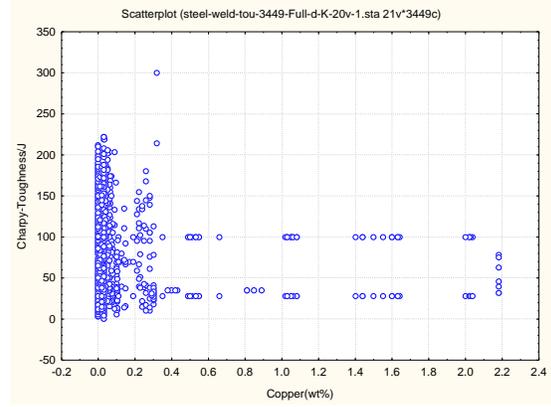
Toughness(J)-Chromium (wt%)



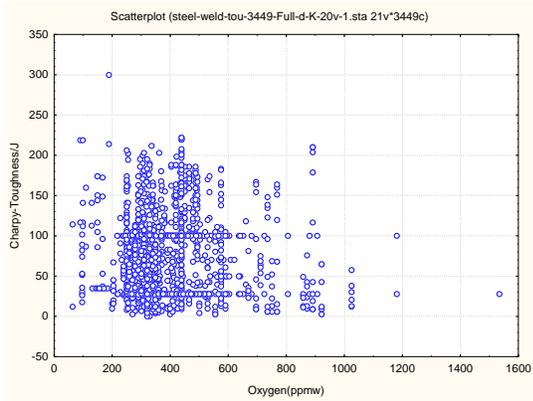
Toughness(J)-Molybdenum (wt%)



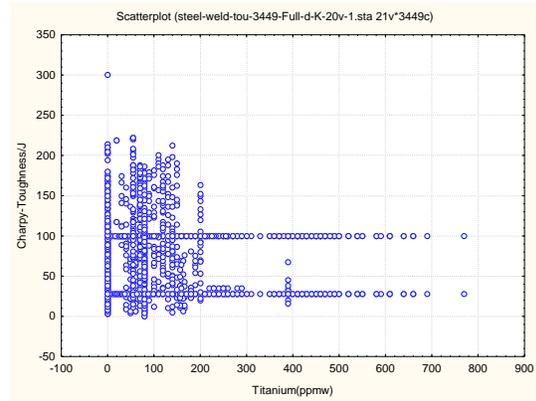
Toughness(J)-Vanadium (wt%)



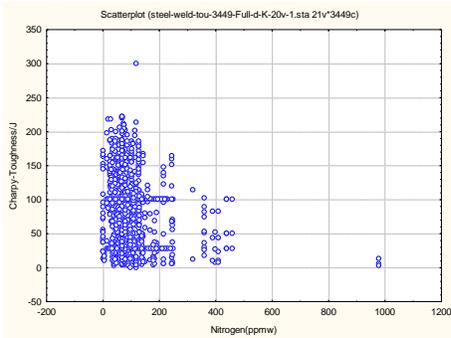
Toughness(J)-Copper (wt%)



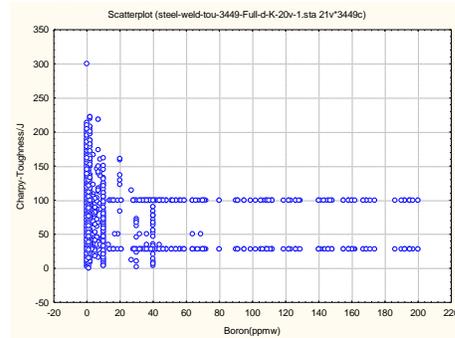
Toughness(J)-Oxygen (ppm)



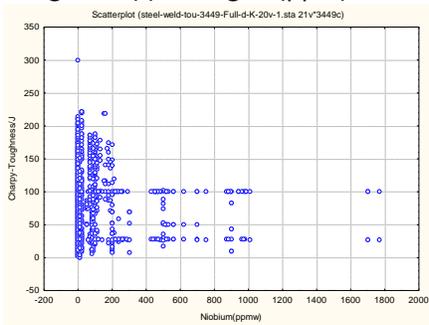
Toughness(J)-Titanium (ppm)



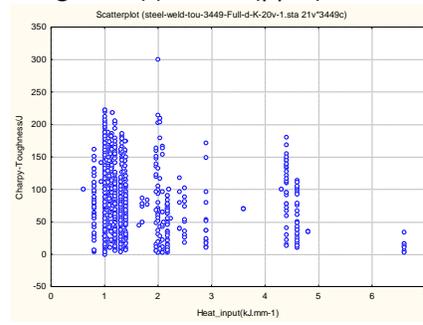
Toughness(J)-Nitrogen (ppm)



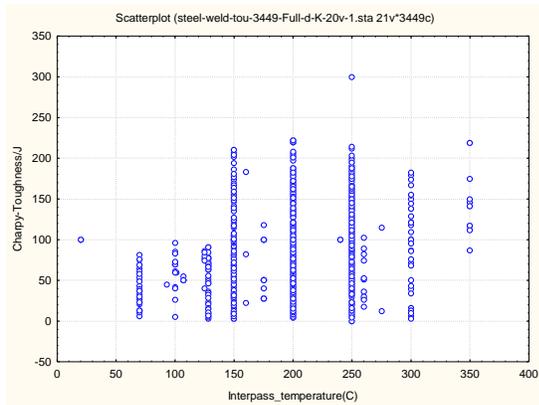
Toughness(J)-Boron (ppm)



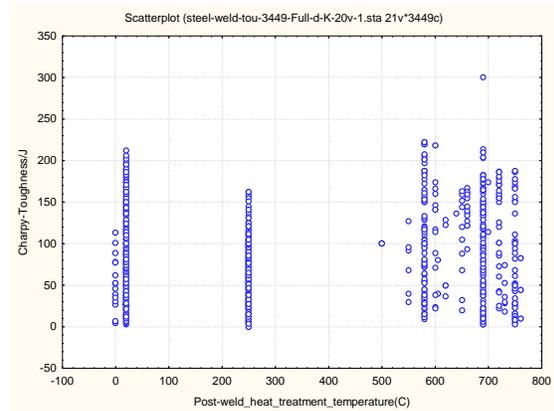
Toughness(J)-Niobium (ppm)



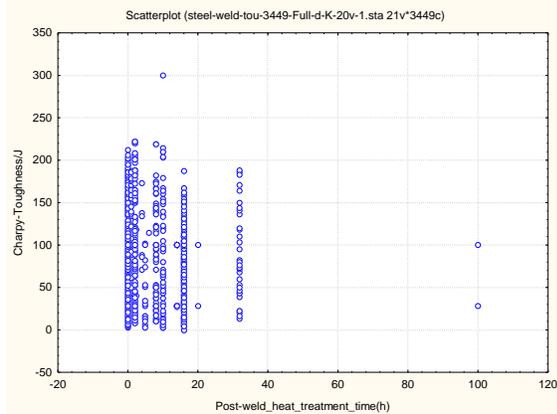
Toughness(J)-Heat Input(KJ mm-1)



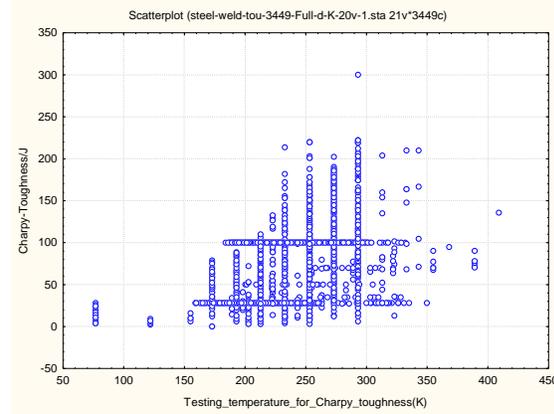
Toughness(J)-Interpass Temperature(C)



Toughness(J)-Post Weld HT Temp(C)



Toughness(J)-Post Weld HT Time(h)



Toughness(J)-Testing Temp-Charpy toughness(K)

Figure 3.13 Database distribution used for **Charpy Toughness** model. “p.p.m .’ corresponds to parts per million by weight.

3.4.2 Neural Network Models for Charpy Toughness

3.4.2.1 Bayesian Neural Network Model and procedure

- 1 Data of charpy toughness were collected and plotted in the form of Scatter plots.
2. Data prepared according to the file format required to run in Neural Network Softwares.

(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)

3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)

4. Data of Ferritic Steel Weld's Charpy Toughness 3449 run in NeuroMat Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.10

Neural network architecture for Bayesian Neural Network was set in NeuroMat Software :

Three layers : **Input Layer**(Input Variables), **Hidden Layer** (Algorithms) and **Output Layer** (Yield Strength)

Algorithms : Bigback 5

5. The data of Ferritic Steel Weld's Charpy Toughness 3449 run in NeuroMat Software with above Neural network architecture for best Neural Network Committee model. The best committee model was decided on the basis of smallest test error of the committee model.

6. For best committee model, the data of Ferritic Steel Weld's Charpy Toughness 3449 run in NeuroMat Software repeatedly hundred of times and finalise the best committee model with smallest test error. (NeuroMat gives in single run set of 100 models which required time in hours. Out of these 100 models, the models in the committee are selected on the basis of smallest test error. The number of models in committee varies everytime with repeatedly running the data in NeuroMat. Thus the selection of committee model with a smallest test error is time consuming.)

Some more than hundred charpy toughness neural network models were trained on a training dataset which consisted of a random selection of 70%of the data 2414 from the charpy toughness dataset. And 20% of the data 690 from charpy toughness data set was used for cross validation.The remaining 345 data formed the test dataset which was used to see how the model generalizes on unseen data. Each model contained the 20 inputs listed in Table 1 but with different numbers of hidden units or the random seeds used to initiate the values of the weights. Fig. 3.14 shows the results. As expected, the perceived level of noise (σ_y) in the normalised charpy toughness decreases as the number of hidden units increases, Fig. 3.14a. This is not the case for the test error, which goes through a minimum at nineteen hidden units, Fig. 3.14b, and for the log predictive error which reaches a maximum at nineteen hidden units, Fig. 3.14c.

The error bars presented throughout this work represent a combination of the perceived level of noise σ_y in the output and the fitting uncertainty estimated from the Bayesian framework. It is evident that there are a few outliers in the plot of the predicted versus measured Charpy Toughness for the test dataset, Fig. 3.14f. Each of these outliers has been investigated and found to represent unique data which are not represented in the training dataset, Fig. 3.14e.

It is possible that a committee of models can make a more reliable prediction than an individual model (Chapter 2). The best models are ranked using the values of the log predictive errors Fig. 3.14c. Committees are then formed by combining the predictions of the best L models, where $L = 1, 2, \dots$; the size of the committee is therefore given by the value of L . A plot of the test error of the committee versus its size gives a minimum which defines the optimum size of the committee, as shown in Fig. 3.14d.

The test error associated with the best single model is clearly greater than that of any of the committees Fig. 3.14d. The committee with eighth models was found to have an optimum membership with the smallest test error. The committee was therefore retrained on the entire data set without changing the complexity of any of its member models.

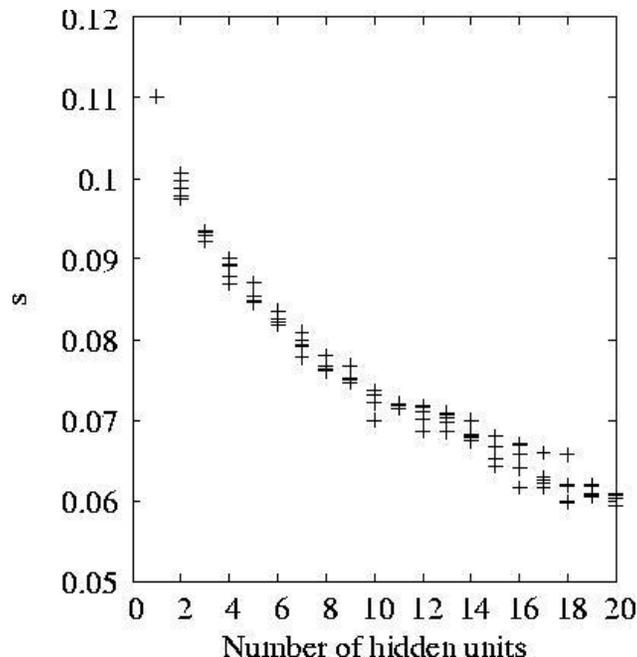


Figure 3.14 (a) σ_y vs Hidden units

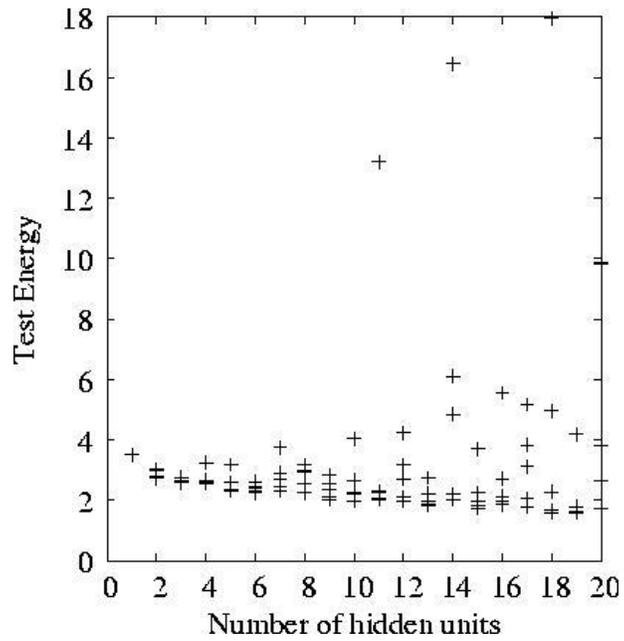


Figure 3.14 (b) Test Error vs Hidden units.

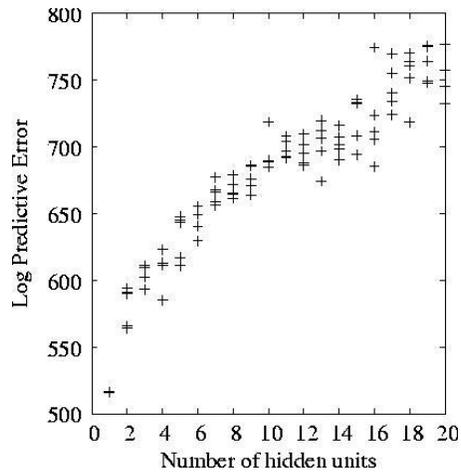


Figure 3.14 (c) Log predictive error vs Hidden units

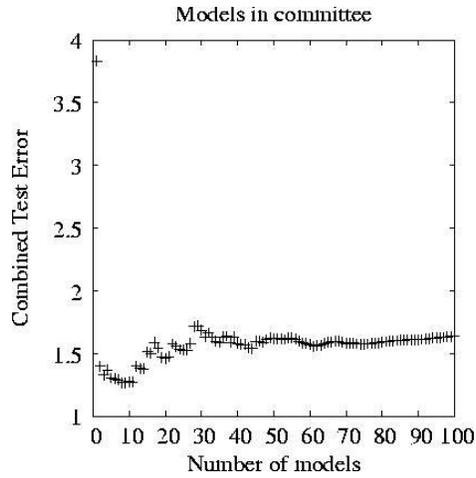


Figure 3.14 (d) Test Error vs Models in committee

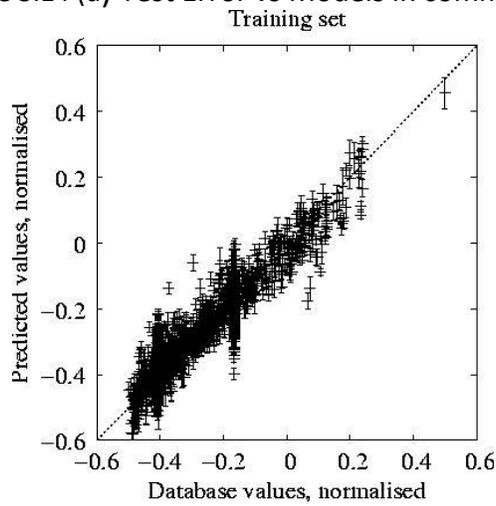


Figure 3.14 (e) Predicted normalized CT. vs Measured normalized CT. (Training Dataset)

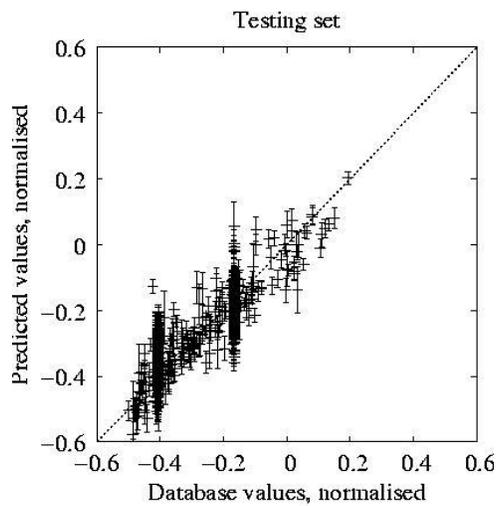


Figure 3.14 (f) Predicted normalized CT. vs Measured normalized CT. (Test Dataset)

Figure 3.14 . (a,b,c,d,e,f) Charpy Toughness (CT) model features.

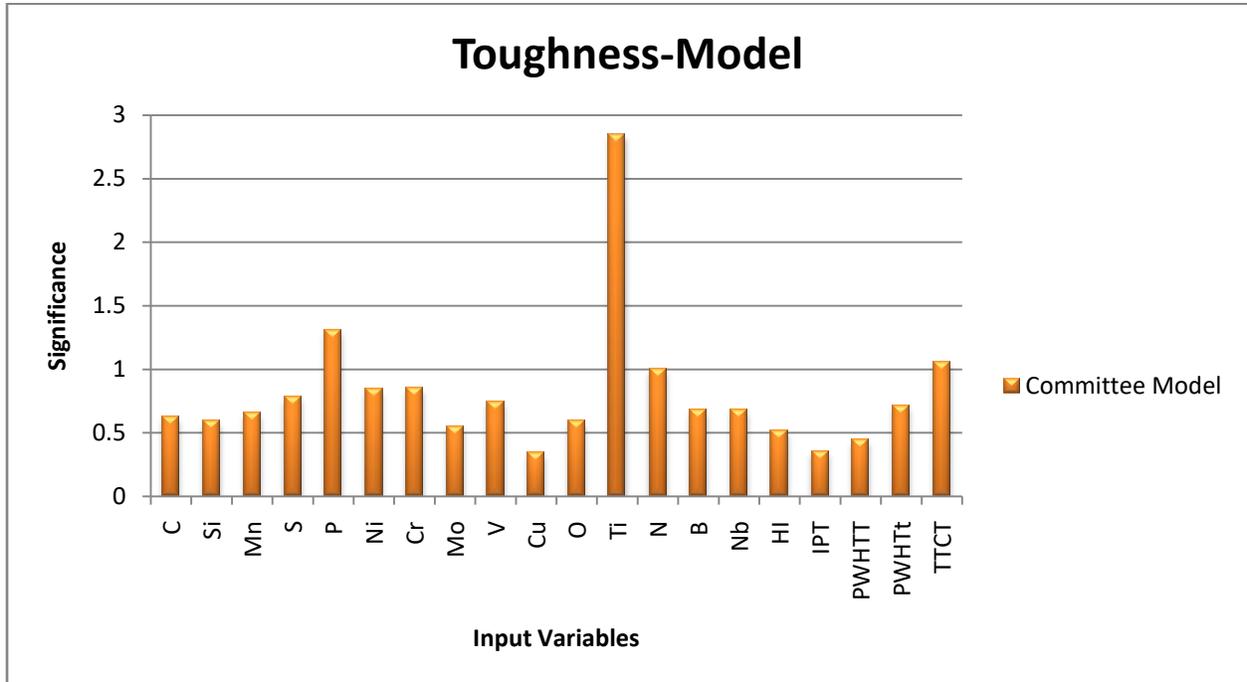


Figure 3.15 The perceived significance σw value of best eight Charpy Toughness models for each of the inputs.

Fig. 3.15 indicates the significance σw of each of the input variables, as perceived by first Eight neural network models in the committee. The σw value represents the extent to which a particular input explains the variation in the output, rather like a particular correlation coefficient in linear regression analysis. The Titanium on the whole explains a large proportion of variation in the Charpy Toughness Figure. 3.15. All variables considered are found to have a significant effect on the output indicating a good selection of inputs.

3.4.3 Comparisons of Neural network models and procedure (MLP, RBF, GRNN)

1 Data of Charpy toughness were collected and plotted in the form of Scatter plots.

2. Data prepared according to the file format required to run in Neural Network Softwares.

(.csv format for Linux base software NeuroMat. And .sta format for Statistica Software)

3. Data were randomly divided into three parts (70% training dataset, 20% validation dataset and 10 % testing dataset). (Training dataset: this data set is used to adjust the weights on the neural network. Validation dataset: this data set is used to minimize overfitting. Testing dataset: this data set is used only for testing the final solution in order to confirm the actual predictive power of the network.)

4. Data of Ferritic Steel Weld's Charpy Toughness 3449 run in Statistica Software, which were set in its hyperparameter or Neural network architecture (Software converts the Raw Data into Normalized condition, i.e. it can convert into a specified range like 0 to 1 etc.. for processing) in Chapter 2.11

Neural network architecture was set in Statistica software for MLP, RBF and GRNN :

MLP 17:17-10-1:1 Algorithms : BP100,CG20,CG18b

RBF 17:17-530-1:1 Algorithms : SS,KN,PI

GRNN 17:17-1061-2-1:1 Algorithms : SS

BP Back propagation, CG Conjugate gradient descent, SS (sub) sample, KN K-nearest neighbor (deviation assignment), PI Pseudo-invert (linear least squares), b Best network (the network with lowest selection error in the run was restored)

A neural network's architecture is of form I:N-N-N:O, where I is the number of input variable, O the number of output variables, N the number of units in each layer.

5. The data of Ferritic Steel Weld's Charpy Toughness 3449 run in Statistica Software with above Neural network architecture for best Neural Network model in all three MLP, RBF and GRNN.

6. For best model, the data of Ferritic Steel Weld's Charpy Toughness 3449 run in Statistica Software repeatedly hundred of times and finalise the best Neural Network model with smallest training error in all three MLP, RBF and GRNN.

7. The neural network model with the smallest training error was the GRNN model.

Table 3.11 shows the comparisons of selected Neural Network models on the basis of their Training Errors. The GRNN models have lowest Training Errors for Charpy Toughness of Ferritic Steel Welds. . The GRNN models are selected for modeling from three basic neural network methods (MLP, RBF, GRNN). Statistica 7.1 software is used for MLP, RBF and GRNN.

Table 3.11 Comparisons of Neural network models (MLP, RBF, GRNN)

Charpy Toughness Models					
SR No.	MLP	Train Error	Test Error	Training/Members	Remarks
1	MLP 20:20-11-1:1 (Model:No.7)	0.090335	0.096968	BP100,CG289b	1 H layer
2	MLP 20:20-14-8-1:1 (Model:No.8)	0.085442	0.093736	BP100,CG488b	2 H layer
3	MLP 20:20-14-8-10-1:1 (Model:No.3)	0.080723	0.091685	BP100,CG499b	3 H layer
Charpy Toughness Models					
SR No.	RBF	Train Error	Test Error	Training/Members	Remarks
1	RBF 20:20-862-1:1 (Model:No.5)	0.07513	0.013794	SS,KN,PI	1 H layer
Charpy Toughness Models					
SR No.	GRNN	Train Error	Test Error	Training/Members	Remarks
1	GRNN 20:20-1725-2-1:1 (Model:No.8)	0.011510	0.0198988	SS	2 H layer
2	GRNN 20:20-1725-2-1:1 (Model:No.16)	0.011953	0.018632	SS	2 H layer
3	GRNN 20:20-1725-2-1:1 (Model:No.7)	0.011404	0.018669	SS	2 H layer
Note: See Appendix C for Profile String of Statistica Neural Network Software					

3.4.4 Best GRNN Model for Charpy Toughness

The normal behavior of the Predicted Charpy Toughness and Observed Charpy Toughness are observed in the Figure. 3.16 for Training data, Validation data and testing data. Training of the model is excellent by GRNN method.

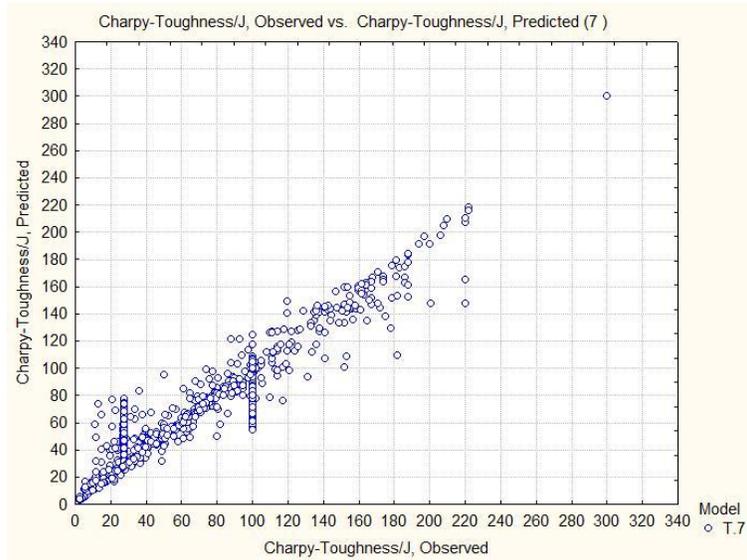


Figure a Training Data for GRNN model of Charpy Toughness

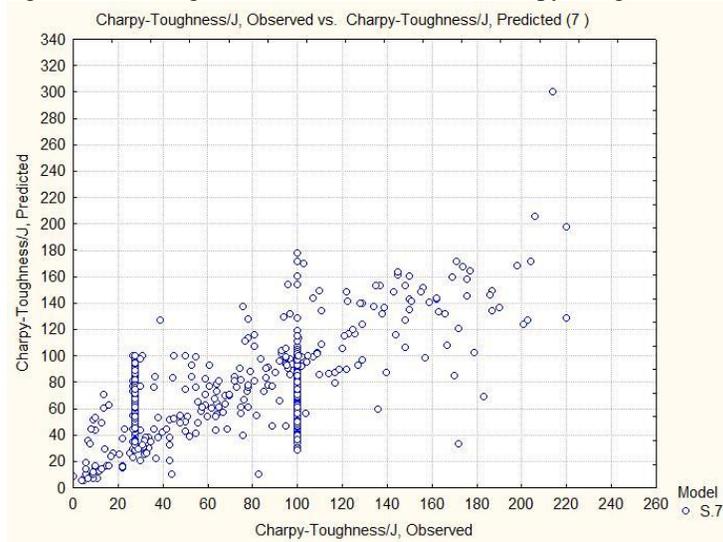


Fig b Validation Data for GRNN model of Charpy Toughness

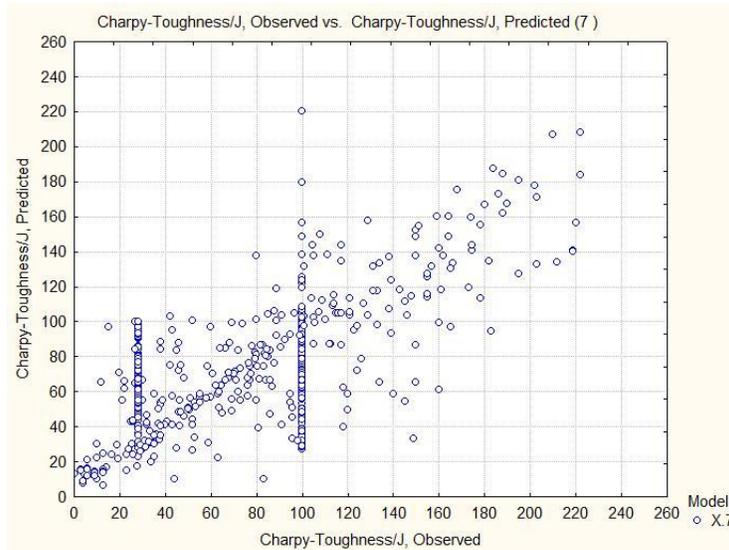


Fig c Test Data for GRNN model of Charpy Toughness

Figure 3.16 (a to c) Training data, validation data and test data of the Best GRNN model for Charpy Toughness.

The best model of GRNN has training error 0.011404, validation error (selection error) 0.018101, and testing error 0.018669. This model is used for getting the results in form of various response graphs to understand the trend between the input variables and output variable (Charpy Toughness).(Figure 4.11 (a to t)).

Table 3.12 Comparison of Significance of Best Trained Models of Elongation

Input Variables	Significance GRNN Model	Significance BNN Model
Carbon(wt%)	7	13
Silicon(wt%)	19	14
Manganese(wt%)	6	12
Sulphur(wt%)	18	7
Phosphorus(wt%)	16	2
Nickel(wt%)	4	6
Chromium(wt%)	10	5
Molybdenum(wt%)	5	16
Vanadium(wt%)	3	8
Copper(wt%)	15	20
Oxygen(ppm)	8	15
Nitrogen(ppm)	14	4
Titanium(ppm)	17	1
Boron(ppm)	20	11
Niobium(ppm)	12	10
Heat_input(kJ.mm-1)	11	17
Interpass_temperature(C)	9	19
Postweld_heat_treatment_temperature(C)	2	18
Post-weld_heat_treatment_time(h)	13	9
Testing Temperature CT (K)	1	3

Table 3.12 shows the comparison of Significance of the GRNN and BNN models. Number 1 indicates highest value of significance and Number 20 lowest value of significance. Most of the Input Variables are not closer in significance for both the models. All input variables considered are found to have a significant effect on the output indicating a good selection of inputs.

3.4.5 Neural Network and Genetic Algorithms Modelling for Charpy Toughness of Ferritic Steel Welds

3.4.5.1 Genetic Algorithms parameters and procedure

A genetic algorithm has been developed in language C considering the following parameters:

Number of populations = 3

Number of generations = 3000

Population size = 20 chromosomes

When a new generation is created, the following steps are followed: after ranking the 20 chromosomes according to their scores, the first chromosome is copied without change. The chromosomes 2 to 19 are recombined with each others. One gene of one of these chromosomes is mutated between $\pm 0.2\%$. The chromosome 20, with the worst score, is killed and a new random chromosome is generated and incorporated in the new population.

This program can calculate the best set (x_1, x_2, \dots, x_j) of input parameters for a desired output y , which is in this study, the charpy toughness of ferritic steel welds, for which a Bayesian neural network model was developed[32].

The steps for Genetic Algorithms Modelling:

- First, all the files related to the neural network created for the charpy toughness were put in the folder "gacode" to optimise. These files were the following:

```
generate44.exe  
norm_test.in  
_w*f  
*.lu  
spec1.tl  
outran.x  
MINMAX
```

- Then, the labels of the inputs variables of the neural network were written in the "labels.tct" file
- Then the all inputs variables were define in the "values" file to vary.
- Then, the desired target value of charpy toughness was normalised and entered it in the "nninput" file, as well as the wanted accuracy.

- Finally, the C program "ga_code" was compiled and executed.

After execution of the Genetic Algorithms program, the output was the values of 20 input variables for given target value of the charpy toughness of Ferritic Steel Weld. The calculation time was in hours.

Three different target values of Ferritic Steel Weld's charpy toughness were taken and Genetic Algorithms programs were run. The outputs were given in result and discussion Chapter 4.